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# BITSAT 2014

## Previous Year Questions

## CHEMISTRY

#### Single correct answer type

1. What will be the product of the reaction?

$$\begin{array}{c} \mathsf{CH}_3\\ \mathsf{I}\\ \mathsf{H}_3\mathsf{C}\text{-}\mathsf{C}\text{-}\mathsf{Br} + \mathsf{Na}\text{-}\mathsf{O}\text{-}\mathsf{CH}_3 \rightarrow\\ \mathsf{I}\\ \mathsf{CH}_3\end{array}$$

 $\begin{array}{c} (A) \begin{array}{c} CH_{3} - C = CH_{2} \\ I \\ CH_{3} \end{array} \end{array} \begin{array}{c} CH_{3} \\ (B) \begin{array}{c} I \\ CH_{3} - O - C - CH_{3} \\ CH_{3} \end{array} \end{array} \begin{array}{c} (C) \\ CH_{3} - CH_{2} - CH_{2} - CH_{3} \\ CH_{3} \end{array} \begin{array}{c} (D) \\ CH_{3} - CH - CH_{3} \\ CH_{3} \end{array} \end{array}$ 

Ans. (A)

- **Sol.** When tertiary alkyl halide is treated with sodium alkoxide than elimination reaction competes over substitution reaction because alkoxides are not only nucleophiles but strong base as well. Therefore, alkenes are formed instead of ethers.
- 2. Which of the following reaction is incorrect regarding Bohr's theory?

(A) Velocity of electron  $\propto \frac{1}{n}$ 

(C) Radius of orbit  $\mu$   $n^2z$ 

Ans. (C)

Sol. Radius of orbit is directly proportional to ration of square of principal quantum number and atomic number

(B) Frequency of revolution ∞

(D) Force on electron or

i.e., Radius of orbit  $\propto \frac{n^2}{z}$ 

For H-atom  $r_n = \frac{n^2 \times 0.529 \times 10^{-8}}{z} \text{cm}$ 

3. Which of the following pair have identical shape?

(A) CH4.SF<sub>4</sub> (B) BCl<sub>3</sub>, CIF<sub>3</sub> (C) XeF2, ZnCl<sub>2</sub> (D) SO2, CO<sub>2</sub>

Ans. (C)

Sol. Molecules /compounds and their shape can be arranged as

Compound	Shape
XeF <sub>2</sub>	Linear
ZnCl <sub>2</sub>	Linear
BCl <sub>3</sub>	Triangular planar
CiF <sub>3</sub>	T-Shaped

Ans.

CH₄	Tetrahedral
SF <sub>4</sub>	See-saw
SO <sub>2</sub>	Bent
CO <sub>2</sub>	Linear

4. 10g of sample of mixture of CaCl<sub>2</sub> and NaCl<sub>2</sub> is treated to precipitate all the calcium as CaCO<sub>3</sub>. This CaCO<sub>3</sub> is heated to convert all the Ca to CaO and the final mass of CaO us 1.62g. The percent by mass of CaCl<sub>2</sub> in the original mixture is

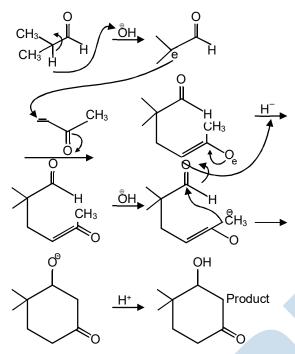
	(A) 32.1%	(B) 16.2%	(C) 21.8%	(D) 12.0%
Ans.	(A)			
Sol.	CaCl <sub>2</sub> + NaCl = 10g			
	Let weight of CaCl <sub>2</sub> = x	g		
	Particle velocity			$\leq$
	$v_{p} = \frac{dy}{dt} = \frac{d}{dt} \bigg[ 3\sin\bigg(25\pi)\bigg]$	$\operatorname{tt}-\frac{\pi}{2}\mathbf{x}\Big]$		
	$v_{p} = 75\pi \cos\left(25\pi t - \frac{\pi}{2}\right)$	x)		OP.
	Maximum particle velo	city, (v <sub>p</sub> ) <sub>max</sub> =75π m/s		
	$\Rightarrow \frac{\left(V_{p}\right)_{max}}{v} = \frac{75\pi}{50}$		¢00	
	$=\frac{3}{2}\pi$			
	Mole of CaO = $\frac{1.62}{56}$			
	$\therefore \frac{x}{111} = \frac{1.62}{56}$			
	x = 3.21g			
	% of CaCl <sub>2</sub> = $\frac{3.21}{10} \times 100$	0 = 32.1%		
5.	How many chiral centre	e are possible for the pro	duct of following reaction	?
	0			

$$\begin{array}{c} CH_{3} \\ CH_{3} \\ H \end{array}^{+} + \underbrace{\longrightarrow}_{O} CH_{3} \\ (i) \text{ Michaell} \\ (i) \text{ OH}^{-} \\ (i) \text{ OH}^{-} \end{array} A$$

$$(A) 1 \qquad (B) 0 \qquad (C) 3 \qquad (D) 2$$

$$(A)$$

Sol. This problems includes conceptual mixing of Michael addition and number of chiral
 Michael addition Addition of nucleophile to enone system is done in such a way that the addition looks like addition at and position of enone is known as Michael addition.



The number of chiral centre in product is 1 represented by star (\*).

6. Elements/ions having same number of electrons are known as isoelectronic species. Arrange the following elements in correct order of atomic/ionic radii and choose the correct choice from the four choices given below

O<sup>2-</sup>, Na<sup>+</sup>, Mg<sup>2+</sup>, F<sup>-</sup>, Al<sup>3+</sup>

(C)  $AI^{3+} > Mg^{2+} > Na^+ > F^- > O^{2-}$ 

D) None of the above

- Ans. (A)
- Sol. Elements/ions having equal number of electrons are known as isoelectronic species. Among isoelectronic species, cations having highest charge are smallest while anion having highest charge are largest.
   Cation < Neutral atom < Anion</li>

Hence, correct choice is  $AI^{3+} < Mg^{2+} < Na^+ < F^- < CO^{2-}$ 

7. The ratio of oxidation states of Cl in potassium chloride to that in potassium chlorate is

(A) 
$$+\frac{1}{5}$$
 (B)  $-\frac{1}{5}$  (C)  $-\frac{2}{5}$  (D)  $+\frac{3}{5}$ 

Ans. (B)

**Sol.** Oxidation state of in Cl in KCl = -1

Oxidation state of Cl in KCLO<sub>3</sub> = +5

 $\therefore$  Ratio of oxidation state of

8. A reaction,  $Cu^{2+} + 2e^- \rightarrow Cu$  is given. For this reaction, graph between Ered versus  $ln[Cu^{2+}]$  is a straight line of intercept 0.34V, then the electrode oxidation potential of the half cell Cu/Cu<sup>2+</sup> (0.1M) will be

(A) 0.35 (B) 
$$0.34 + \frac{0.0591}{2}$$
 (C)  $-0.34 - \frac{0.0591}{2}$  (D)  $-0.34 + \frac{0.0591}{2}$ 

Ans. (D)

**Sol.**  $Cu^{2+} + 2e^{-} \rightarrow Cu$ 

$$\mathsf{E}_{cu^{2+}/Cu} = \mathsf{E}_{Cu^{2+}/Cu}^{0} - \frac{0.059}{2} log \frac{1}{\left[Cu^{2+}\right]}$$

 $=\mathsf{E}_{\mathsf{cu}^{2^{+}}/\mathsf{Cu}}-\frac{\mathsf{RT}}{2\mathsf{F}}\mathsf{In}\Big[\mathsf{Cu}^{2^{+}}\Big]$ 

Intercept =0.34  $\Rightarrow$   $E_{Cu^{2+}/Cu} = 0.34$ 

$$E_{cu^{2+}/Cu} = 0.34 + \frac{0.059}{2} \log 0.1 = 0.31 V$$

$$\mathsf{E}_{cu/Cu^{2+}} = -\mathsf{E}_{Cu^{2+}/Cu} = -0.34 + \frac{0.059}{2}\mathsf{V}$$

9. Which one of the following silanes on hydrolysis produces cross linked polymers?

(B) R<sub>2</sub>SiCl<sub>2</sub>

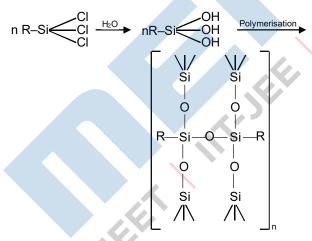
(C) R<sub>3</sub>SiCl

(D) R<sub>4</sub>Si

(A) RSiCl₃

Ans. (A)

**Sol.** RSiCl<sub>3</sub> on hydrolysis produces cross linked polymer.

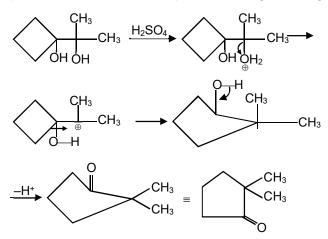


**10.** Identify the correct product formed during the following reaction.

$$(A) \bigvee_{O} \bigvee_{CH_{3}}^{CH_{3}} (B) \bigvee_{CH_{3}}^{CH_{3}} (C) \bigvee_{O} \overset{CH_{3}}{CH_{3}} (D) \bigvee_{CH_{3}}^{CH_{3}} (C) \bigvee_{O} \overset{CH_{3}}{CH_{3}} (D) \bigvee_$$

### Ans. (D)

**Sol.** <b>Pinacol-pinacolone rearrangement</b> The diol is converted into  $\alpha$  -hydroxy ketone when reacted in presence of acid is believe to proceeds through rearrangement of carbocation as shown.



Relief from angle strain

Basic of carbocationic rearrangement is due to relief from angle strain.

- 11. Usually, CaCl<sub>2</sub> is preferred over NaCl for cleaning snow on roads particulary in very cold countries. This is because
  - (A) NaCl makes the road slippery but CaCl<sub>2</sub> does not
  - (B) CaCl<sub>2</sub> is hygroscopic but NaCl is not
  - (C) CaCl<sub>2</sub> is less soluble in H<sub>2</sub>O than NaCl
  - (D) Eutectic mixture of CaCl<sub>2</sub>/H<sub>2</sub>O freezes at -55°C while that of NaCl/H<sub>2</sub>O freeze at -18°C.
- **Ans.** (D)
- Sol. A mixture of chemical compounds having a single chemical composition, solidifies at a lower temperature than any other composition made up of the same ingredients. This mixture is called eutectic mixture. Freezing point eutectic mixture of NaCl/H<sub>2</sub>O is only -180°C but the ambient temperature of very cold countries is much lower than -180°C. In such situations, NaCl will be ineffective. Thus, for such situations eutectic mixture CaCl<sub>2</sub>/H<sub>2</sub>O is used because it has freezing point of -55°C which is much lower than NaCl. This mixture lowers the freezing point of ice that allows street snow or ice to melt at lower temperature.
- 12. The gold numbers of a few protective colloids are given
  - x 0.005
  - y 3.5
  - z 40

The protective nature of these colloidal solutions follow the order

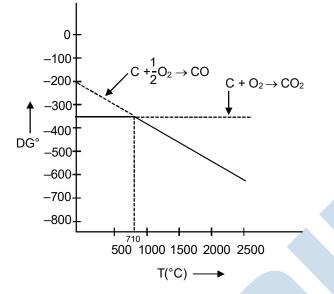
	(A) Z > x > y	(B) x < y > z	(C) z > y > x	(D) x > y > z
Ans.	(D)			

Sol. Smaller the gold number, greater is its protective power. Hence, the order would be

x > y > z

<b>Caution Point</b> Gold number is used for calculating the protective powers of lyophilic colloids.

**13.** Consider the following Ellingham diagram for carbon



Which of the statement is incorrect for the above Ellingham diagram?

(A) Upto 710°C, the reaction of formation of  $CO_2$  is energetically more favourable but above 710°C, the formation of CO is preferred

(B) Carbon can be used to reduce any metal oxide at a sufficiently high temperature

(C) Carbon reduces many oxides at elevated temperature because  $\Delta G^{\circ}$  vs temperature line has a negative slope

(D) 
$$\Delta S^0 \left[ C(s) + \frac{1}{2}O_2(g) \rightarrow CO(g) < \Delta S^0 \left[ C(s) + O_2(g) \rightarrow CO(g) \right] \right]$$

Ans. (D)

**Sol.** Since, 
$$\Delta G^{\circ} = \Delta H^{\circ} - T \Delta S^{\circ}$$

Where,  $\Delta G^{\circ}$  = standard Gibb's free energy of the reaction

 $\Delta G^{\circ}$  = standard entropy of the reaction

 $\Delta H^{\circ}$  standard enthalpy of the reaction

T = temperature

From, the above equation, it is clear that,  $\Delta G^{\circ}$  will be more negative when  $\Delta S^{\circ}$  is less negative (or  $\Delta S^{\circ}$  is high).

In the diagram,  $\Delta G^{\circ}$  value for  $C + \frac{1}{2}O_2 \rightarrow CO$  is less negative, (lower) than that for  $C + O_2 \rightarrow CO_2$ 

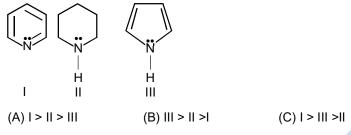
Therefore,  $\Delta S^{\circ}$  would be higher for

 $C + \frac{1}{2}O_2 \rightarrow CO$ 

Than that for C +  $O_2 \rightarrow O_2$ 

Hence, 
$$\Delta S^{\circ} \left[ C(s) + \frac{1}{2}O_{2}(g) \rightarrow CO(g) \right] > \Delta S^{\circ} \left[ C(s) + O_{2}(g) \rightarrow CO(g) \right]$$

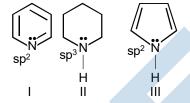
14. Arrange the following in correct order of basicity



Ans. (C)

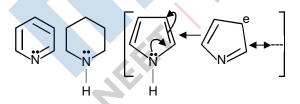
**Sol.** This problem includes conceptual mixing of basic strength, hybridization of nitrogen atom and extent of conjugation.

While solving such problem students are advised to draw the structure and mark the type of hybridization on N-atom, then answer the question by using combined concept of hybridization and conjugation. Hybridization of N-atom in below compounds are sp<sup>2</sup>, sp<sup>3</sup> and sp<sup>2</sup> respectively.



Greater the s-character more will be electronegativity of N-atom and lesser will be its basicity on this basic I is less basic than II.

<b>Conjugation</b> If lone pairs of electron of N is involved in conjugation causes decrease in basicity of compound due to lesser availability of lone pair for donation to show basic nature.



Lone pair involved in formation of aromatic sextet of  $6\pi$  - electron (least basic).

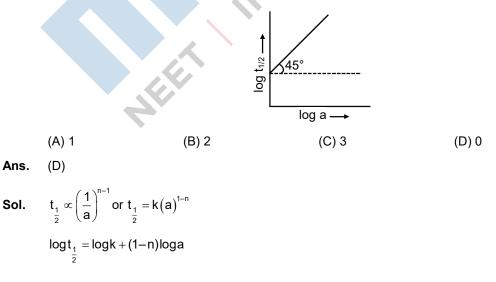
- **15.** What is the density of Na<sub>2</sub>O having antifluorite type crystal structure, if the edge length of the cube is 100pm and what is the effect on density by 0.05% Frenkel defect?
  - (A) 823.5 g cm<sup>-3</sup> density increases
  - (C) 823.5 g cm<sup>-3</sup>, density remains same (D) 414.16 g cm<sup>-3</sup>, density remains same
- (B) 414.16 g cm<sup>-3</sup>, density decreases
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Ans. (D)  
Sol. As, density 
$$(p) = \frac{Z_{aff} * Molecular weight}{N_{b} \times a^{2}}$$
  
(For antifluorite,  $p = \frac{4 \times (23 \times 2 + 16)}{6 \times 10^{3} \times (100 \text{ m} \times 10^{-13})^{3}}$   
= 414.16 g cm<sup>-3</sup>  
[1 picometer = 10<sup>-12</sup> m = 10<sup>-10</sup> cm]  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  
  

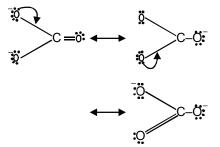
18. Mercury is a liquid metal because (A) It has a completely filled d-orbital that causes d-d overlapping (B) It has completely filled d-orbital that prevents d-d overlapping (C) It has a completely filled s-orbital (D) It has a small atomic size Ans. (B) The electronic configuration of mercury is [Xe]4f<sup>10</sup>, 5d<sup>10</sup>, 6s<sup>2</sup>. Its d-subshell is completely filled, thus, it Sol. prevents the overlapping of d-orbitals (d-d overlapping). Hence, it is liquid metal at room temperature. 19. The volume of 10N and 4N HCl required to make 1L of 7N HCl are (A) 0.75 L of N HCl and 0.25 L of 4 N HCl (B) 0.50 L of 10 N HCl and 0.50 L of 4 N HCL (C) 0.65 L of 10 N HCl and 0.5 L of 4 N HCl (D) 0.85 L of 10 N HCl and 0.15 L of 4 N HCl Ans. (B) Let V litre of 10 N HCl be mixed with (1 - V) litre of 4 N HCl to give (V + 1 - V) = 1 L of 7N HCl Sol. As we know that, OUNDA  $N_1V_1 + N_2V_2 = NV$  $10V + 4(1 - V) = 7 \times 1$ 10V + 4 - 4V = 76V = 7 - 4 $V = \frac{3}{6} = 0.50L$ Volume of 10 N HCl = 0.50 L Volume of 4 N HCl = 1 - 0.50 = 0.50 L

**20.** Following is the graph between  $\log T_{50}$  and  $\log a(a = initial concentration)$  for a given reaction at27°C. Hence, order is



	(It represents straight line equation; $y = c + mx$ )					
	Slope = $(1 - n) = \tan 45^\circ = 1$					
	$\therefore (1 - n) = 1$					
	$\Rightarrow$ n =0					
21.	The catalyst used for olefin polymerization is					
	(A) Ziegler-Natta catalyst (I	(B) Raneynickel catalyst				
	(C) Wilkinson catalyst (I	(D) Merrified resin				
Ans.	. (A)					
Sol.	Ziegler-Natta catalyst [TiCl <sub>4</sub> + Al $(C_2H_5)_3$ ] is used a	as a catalyst in the polymerization of olefins.				
22.	Which one of the following is a covalent hydride?					
	(A) CaH <sub>2</sub> (B) NaH (9	(C) BH <sub>3</sub> (D) BeH <sub>2</sub>				
Ans.						
Sol.	Hydrides are binary compounds of hydrogen. The	ese can be classified into four groups				
	(i) Ionic hydrides : NaH, CaH <sub>2</sub> , LiH					
	(ii) Covalent hydrides: B <sub>2</sub> H <sub>6</sub> , NH <sub>3</sub> , NaBH <sub>4</sub>					
	(iii) Polynuclear hydrides : LiAlH₄, NaBH₄					
		ogen is trapped in the interstitial spaces of transition				
	metals.	lently apphied with enother DLL melecule to form				
	B <sub>2</sub> H <sub>6</sub> .B <sub>2</sub> H <sub>6</sub> contain 3 centre 2e <sup>-</sup> bonds.	alently combined with another $BH_3$ molecule to form				
23.	Which one of the following is used for the separati	tion of noble gas mixture from air?				
	(A) Charcoal	(B) 90%CaC <sub>2</sub> + 10%CaCl <sub>2</sub>				
		(D) 90%CaCO₃ + 10% urea				
Ans.	. (B)					
Sol.	The method used to separate noble gas mixture fro	om air is called <b>Fischer-Ringe's</b> method. When				
	air free from moisture and $CO_2$ is passed over a he	eated mixture (800°C) of 90% $CaC_2$ + 10% $CaCI_2$ in an				
	iron sealed tube, the following reactions take place	e				
	$CaC_2 + N_2 \xrightarrow{800^{\circ}C} CaCN_2 + C$					
	$2C + O \rightarrow 2CO$					
	$C + O_2 \rightarrow CO_2$					
	$2CaC_2 + 3CO_2 \rightarrow 2CaCO_3 + 5C$					
	$CuO + CO \rightarrow Cu + CO_2$					
	CO <sub>2</sub> gas is absorbed by KOH solution. Thus, a mix	ixture of inert gases are obtained.				

- 24. Consider the following statements.
  - I. NCl<sub>5</sub> does not exist while  $PCl_5$  does.
  - II. Both  $O_2^+$  and NO are paramagnetic.
  - III. The three C O bonds are not equal in carbonate ion.
  - IV. Head prefers to form tetravalent compound. Which of the above statements are incorrect?
  - (A) I and III (B) I, III and IV (C) II and III (D) III and IV
- Ans. (D)
- Sol. I. In nitrogen, d-orbitals are absent, hence, it does not form NCl<sub>5</sub>. Thus, NCl<sub>5</sub> does not exist but PCl<sub>5</sub> does.
  - II.  $O_2^+$  and NO are isoelectronic and contains one unpaired electron each. Thus, both are paramagnetic.
  - III. In carbonate ion.  $CO_3^{2-}$  all three C –O bonds are identical due to resonance



IV. Pb<sup>2+</sup> is more stable than Pn<sup>4+</sup> due to inert pair effect, hence, prefers to form divalent compounds. Thus, the incorrect statements are III and IV.

- 25.
   The liquefied metal that expand on solidification is

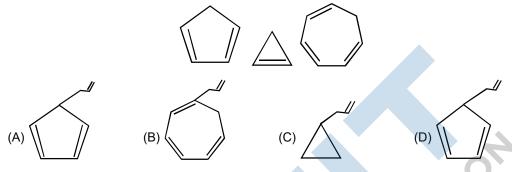
   (A) AI
   (B) Zn
   (C) Ga
   (D) Cu
- Ans. (C)
- **Sol.** Gallium, Ga is a soft silvery white metal and is liquid at room temperature. When it solidifies, expands by 3.1%. Thus, it should not be stored in glass or metal containers.
- 26. Point out the correct statement for the set of characteristics of ZnS crystal.
  - (A) Coordination number (4 : 4); ccp;  $Zn^{2+}$  ion in the alternate tetrahedral voids
  - (B) Coordination number (6 : 6); hcp; Zn<sup>2+</sup> ion in all tetrahedral voids
  - (C) Coordination number (6 : 4); hcp; Zn2+ ion in all octahedral voids
  - (D) Coordination number (4 : 4); ccp; Zn<sup>2+</sup> ion in all tetrahedral voids
- Ans. (A)
- Sol. Zns has zinc blende type structure (i.e., ccp structure). The S<sup>2-</sup> ions are present at the corners of the cube and at the centre of each face. Zinc ions occupy half of the tetrahedral sites. Each zinc ion is surrounded by four sulphide ions which are disposed towards the corner of regular tetrahedron. Similarly, S<sup>2-</sup> ion is surrounded by four Zn<sup>2+</sup> ions.

27.	Arrange the following compounds in the increasing order of nucleophilic addition reaction.							
	І. НСНО	II.CH <sub>3</sub> COCH <sub>3</sub>	III.C <sub>6</sub> H₅COCH <sub>3</sub>	$IV.C_3H_5COC_6H_5$				
	(A)   <    <     <  V	(B) IV < III < II <i< th=""><th>(C) IV &lt;    &lt;     &lt;  </th><th>(D)     &lt;  V &lt;    &lt;  </th></i<>	(C) IV <    <     <	(D)     <  V <    <				
Ans.	(C)							
Sol.	Reactivity of nucleop	hilic addition reaction de	epends upon the electro	n deficiency of carbonyl group and				
	steric hinderance. Ste	eric hinderance decrease	es the rate of reaction. T	his steric hinderance is minimum in				
	methanol and maxim	um in benzophenone.						
28.				e is 1348.9 kcal mol⁻¹ at 25°C, then				
		t constant pressure whe		(D) None of the above				
Ans.	(A) –1348.9 kcal	(B) –1342.34 kcal	(C) +1250 kcal	(D) None of the above				
Sol.	(B)	ation of quoroop in C. H.	$_{2}O_{11}(s) + 120_{2}(G) \rightarrow 120$	$20.(a) \pm 114.0(a)$				
501.			$_{2O_{11}(S)} + 12O_{2}(G) \rightarrow 12C$	5O <sub>2</sub> (g) + TH <sub>2</sub> O(g)				
	Here, ∆n = 12 + 11 –	12 = 11						
	As we know, $\Delta H = \Delta E + \Delta nRT$							
	$DH = (-1348.9 \times 10^3) + 11 \times 2 \times 298$							
	= -1348900 + 6556 = -1342344 cal							
	=-1342.344 kcal							
	1342.344 Koai							
29.	Arrange the following	compounds in increasir	ng order of their boiling p	points				
-	СН3							
	I. CH−CH₂I	3r						
	CH <sub>3</sub>							
	II. CH <sub>3</sub> CH <sub>2</sub> –CH <sub>2</sub> –CH <sub>2</sub>	-Br						
	CH <sub>3</sub>							
	III. CH <sub>3</sub> —Ċ—CH <sub>3</sub>							
	Br							
	(A)    <   <	(B) I < II < III	(C)     <   <	(D) III < II < I				
Ans.	(C)							
Sol.	Boiling point decreases with increase in branching. Compound (III) has two branches, compound (I) has							

- **Sol.** Boiling point decreases with increase in branching. Compound (III) has two branches, compound (I) has one branch and compound (II) is a normal alkyl halide with no branch. So, the boiling point is minimum for compound (III) and maximum for compound (II).
- $30. \qquad \mbox{Which of the following compounds will give positive iodoform test with I_2 and NaOH?} \\ (A) C_6H_5COC_6H_5 \qquad (B) CH_3CH_2CHO \qquad (C) C_6H_4COCH_2CH_3 \qquad (D)$

(D) Ans.

- Aldehydes and ketones posses ( $-C-CH_3$ ) group will give positive iodoform test, A part from methylated Sol. carbonyl compounds, alcohols with CH3-CHgroup also give positive iodoform test. ĊН
- 31. What will be the product when most acidic species among following will react with 3-chloroprop-1-ene?

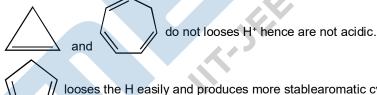


(A) Ans.

Sol. This problem includes conceptual mixing of acidic character, aromaticity and nucleophilic substitution reaction.

Student are advised to identify the most stable intermediate obtained among all (after the removal of H<sup>+</sup>) keeping in mind the concept of conjugation and aromaticity. Then complete the reaction further using concept of nucleophilic substitution reaction.

<b>Acidic character</b> The species which easily donate its hydrogen and produces stable conjugate base is acid. The species which produces more stable conjugate base is more stronger acid.

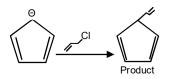


looses the H easily and produces more stablearomatic cyclopentadienyl anion.

Aromatic Non-aromatic

(cyclopentadienyl anion)

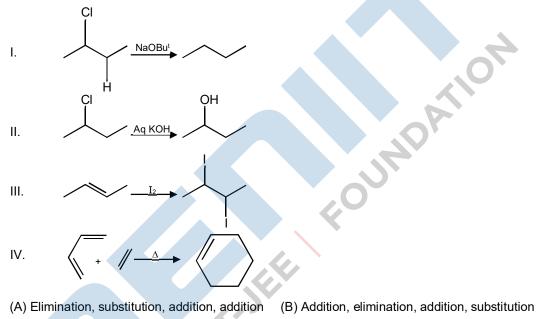
Now, cyclopentadienyl anion on reaction with 3-chloro prop-1-ene produces the product via nucleophilic substitution reaction.



32.	$CaCO3(s) \xrightarrow{Heat} X(s) + Z(g)$							
	$X(s) \xrightarrow{Carbon.heat} C(s) + D(g)$							
	$C(s) + H_2O \rightarrow E(g).$							
	(A) C <sub>2</sub> H <sub>2</sub> , CaO	(B) C <sub>2</sub> H <sub>2</sub> , CaC <sub>2</sub>	(C) CH <sub>4</sub> , CaC <sub>2</sub>	(D) CH <sub>4</sub> , CaO				
Ans.	(B)							
33.	Which of the following	will not form optical isom	ers?					
	(A) [Co(en)₃] <sup>3+</sup>		(C) [Pt(en) <sub>2</sub> Cl <sub>2</sub> ] <sup>2+</sup>	(D) [CrCl <sub>2</sub> (ox) <sub>2</sub> ] <sup>3-</sup>				
Ans.	(B)							
Sol.				try. Complex [Co (NH <sub>3</sub> ) <sub>3</sub> (NO <sub>2</sub> ) <sub>3</sub> ]				
	shows facial and meric will not form optical iso		omers of this complex c	ontain place of symmetry. So, it				
	····· ····							
34.	The true statement abo	out the product is						
	(A) It does not exist as	Zwitter ion						
	(B) It does not act as ir	nner salt						
	(C) $-SO_3$ diminishes th	e basic character of –NH	H <sub>2</sub>	0'				
	(D) –NH <sub>2</sub> displays a po	werful basic character						
Ans.	(C)							
	ŅH₂ I	NH <sub>2</sub> ×H <sub>2</sub> SO <sub>4</sub>	NHSO3H NH2	NH <sup>±</sup>				
	H <sub>2</sub> SO <sub>4</sub>	180°C		$\bigtriangleup$				
			$O \rightarrow O$					
	$\sim$		$\checkmark$	$\uparrow$				
Sol.			SO <sub>3</sub> H	SO₃				
			as acidic as well as basi	c groups in the same molecule.				
	Such ions are called Z	witter ions or inner salts.						
35.	A copolymer of ethere	and vinyl chloride conta	ains alternate monomers	of each type. What is the mass				
		oride in this copolymer?						
	(A) 38%	(B) 69%	(C) 72%	(D) 82%				
Ans.	(B)							
Sol.	The structure of copoly	mer of ethane and vinyl	chloride is shown below					

n(CH<sub>2</sub>=CH<sub>2</sub>) + n (CH<sub>2</sub>=CHCI) Ethene vinyl chloride CH<sub>2</sub>—CH<sub>2</sub>-copolymer Molecular weight of ethane (CH<sub>1</sub>CH<sub>2</sub>) = 28 Molecular weight of vinyl chloride (CH<sub>2</sub>CHCl) = 62.5 Empirical formula weight of copolymer = 28 + 62.5 = 90.5 Mass % of vinyl chloride in the copolymer =  $\frac{62.5 \times 100}{90.5} = 69.06 \approx 69\%$ 36. The number of disulphide linkages present in insulin are (A) 1 (B) 2 (D) 4 (C) 3 Ans. (B) Insulin is composed of two peptide chains referred to chain A and B. Chain A of 21 residues and chain B Sol. of 30 residues are cross linked by two disulphide bridges. 37. Which of the following statement is not true about the drug barbital? (A) It is used in sleeping pills (B) It is a non-hypnotic drug (C) It is transquilizer (D) It causes addiction Ans. (B) Barbital is a sleep-producing drug, hypnotic tranquillizer. It causes addition. Sol. 38. Calculate the pH at the equivalence point during the titration of 0.1M, 25 mL Ch3COOH with 0.05 M NaOH solution. (Ka (CH3COOH) = 1.8 × 10-5) (A) 9.63 (B) 8.63 (C) 10.63 (D) 11.63 Ans. (B) Since, at equivalence point (for acid) Sol. =  $N_2V_2$  (for base) :. Volume of NaOH required to reach equivalence point  $=\frac{0.1 \times 25}{0.05} = 50 \text{ mL}$  $\therefore \text{ Concentration of salt formed} = \frac{\text{millim olers of acid}}{\text{total volume inmL}} = \frac{25 \times 0.1}{75} = \frac{0.1}{3}$ Since,  $\left[H^{+}\right] = \sqrt{\frac{K_{w} \times K_{a}}{c}} = \sqrt{\frac{10^{-14} \times 1.8 \times 10^{-5} \times 3}{0.1}}$ ∴ pH = 8.63

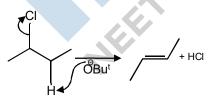
- 39. The temperature 30.98°C is called critical temperature (T<sub>C</sub>) of carbon dioxide. The critical temperature is the
  - (A) Lowest temperature at which liquid carbon dioxide is observed
  - (B) Highest temperature at which gas carbon
  - (C) Highest temperature at which solid carbon dioxide is observed
  - (D) Highest temperature at which liquid carbon dioxide is observed
- Ans. (D)
- **Sol.** Critical temperature of a gas is highest temperature at which liquification of the gas first occurs. The temperature 30.98°C is called critical temperature of carbon dioxide because this is the highest temperature at which liquid carbon dioxide is observed. Above this temperature it is gas.
- 40. The type of reactions for these are



(C) Elimination, addition, substitution, addition (D) Substitution, elimination, addition, addition

Ans. (A)

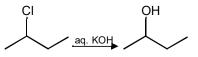




The reaction in which smaller neutral molecule are removed during the reaction is known as elimination reaction.

II. <b>Substitution reaction</b> The reaction in which one nucleophilic group is replaced by another nucleophile is known as nucleophilic substitution reaction.

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Here, OH replaces Cl.

III. <b>Addition reaction</b> The reaction in which reactant undergo addition with reagent to given a single product.

 $\mathbf{I}_2$ 

IV. <b>Addition reaction</b>

Hence,

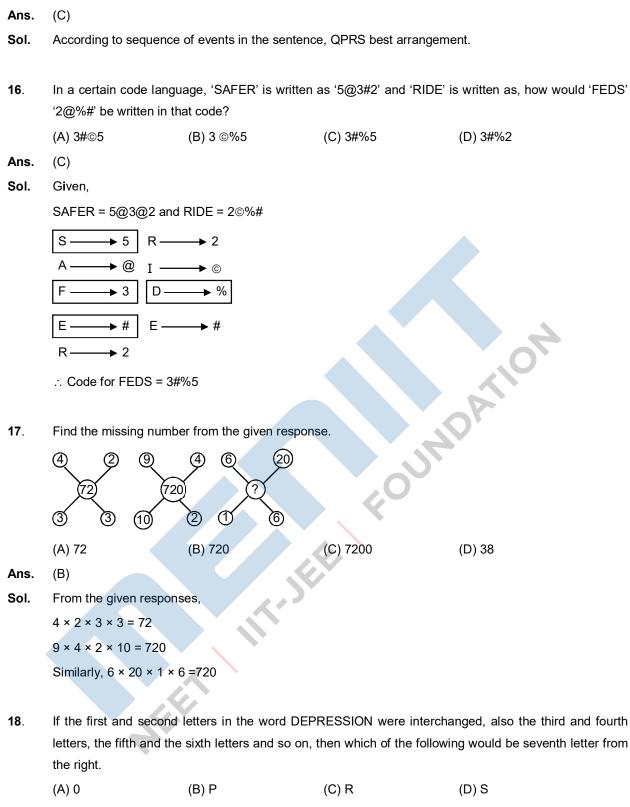
 $I_2$ FOUNDATI FE

## ENGLISH

Single	Single correct answer type							
1.	<b>Out of the four alternatives, choose the one which express the right meaning of the word. </b>							
	<b>Augment</b>							
	(A) Increase	(B) Decrease	(C) Save	(D) Mention				
Ans.	(A)							
Sol.	Augment means make	bigger, so increase is the	e correct option.					
2.	<b>Out of the four alte</b>	rnatives, choose the one	which express the right	meaning of the word.				
	<b>Consolation</b>							
	(A) Comfort	(B) Problem	(C) Sadness	(D) Solution				
Ans.	(A)							
Sol.	Consolation means 'co	mfort received by a perso	on after a loss', so comfo	ort is correct option.				
3.	<b>Out of the four alte</b>	rnatives, choose the one	which express the right	meaning of the word.				
	<b>Auxiliary</b>							
	(A) Chief	(B) Supplemental	(C) Negligible	(D) Separate				
Ans.	(B)							
Sol.	Auxiliary means 'provid	ling additional help', so s	upplemental is correct o	otion.				
4.	<b>Choose the word a</b>	pposite meaning to the g	iven word.					
	<b>Auspicious</b>		6.					
	(A) Prosperous	(B) Unfavourable	(C) Improper	(D) New				
Ans.	(B)							
Sol.	Auspicious means 'favo	ourable', so 'unfavourable	e' is best opposite word	for it.				
5.		pposite meaning to the g	jiven word.					
	<b>Recompense</b>							
	(A) Emolument	(B) Reward	(C) Payment	(D) Penalty				
Ans.	(D)							
Sol.	Recompense means 'p	ayment', so 'penalty' is t	he correct opposite word	for it.				
6.		pposite meaning to the g	iven word.					
	<b>Impede</b>							
	(A) Block	(B) Delay	(C) Push	(D) Freeze				

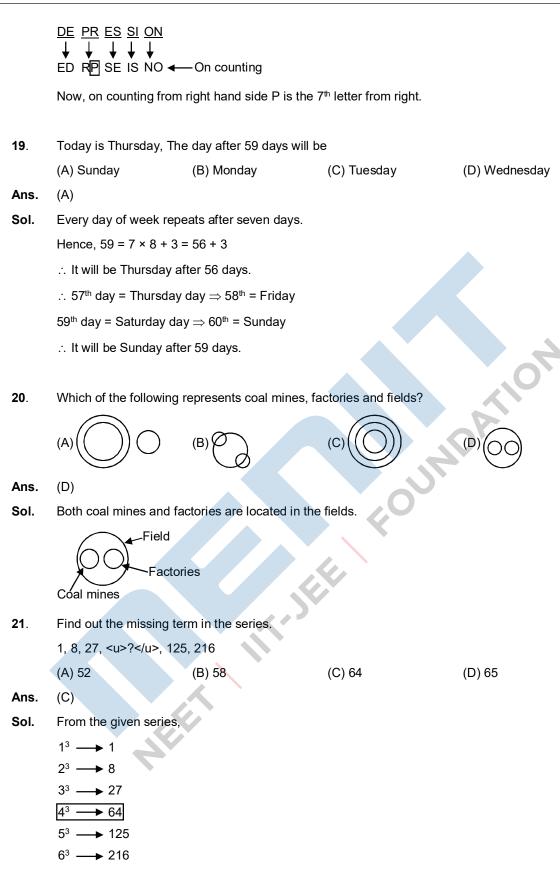
Ans.	(C)						
Sol.	Impede means 'hinder' or 'obstruct', so 'push' is correct opposite word for it.						
7.	A part of sentence is underlined. Balance are given alternatives to the underlined part a, b, c and d which						
	many improve the sentence. Choose the correct alternative.						
	They <u>requested<!--</th--><th>u&gt; me to follow them</th><th></th><th></th></u>	u> me to follow them					
	(A) Ordered	(B) Urged	(C) Asked	(D) No improvement			
Ans.	(A)						
Sol.		mand is depicted in sent	ence, so we should use	'ordered' for proper meaning of			
	sentence.						
8.		Inderlined. Balance are g Itence. Choose the corre		nderlined part a, b, c and d which			
	She did not <u>believ</u>		ct alternative.				
	(A) Believing	(B) Believe to	(C) Believe	(D) No improvement			
Ans.	(C)						
Sol.		ense and V₁ is used in t	hose sentence which co	ntain 'did', so option (believe) is			
	correct.						
			5.				
9.	A part of sentence is u	Inderlined. Balance are g	iven alternatives to the ur	nderlined part a, b, c and d which			
	many improve the sen	tence. Choose the corre	ct alternative.				
	I am fine, what about	<u>you?</u>					
	(A) Your	(B) Your's	(C) Yours	(D) No improvement			
Ans.	(D)						
Sol.	No improvements is n	eeded as sentence is rig	ht.				
10.	<b>Sentence Comple</b>	tion					
	They were afraid	the lion, so they dro	pped the idea of hunting	in jungle.			
	(A) in	(B) to	(C) from	(D) to			
Ans.	(D)						
Sol.	Afraid agrees with pre	position 'of', so option (to	) is correct.				
11.	<b>Sentence Comple</b>						
	Our company signed a	a profitable last me	onth.				
	(A) issue	(B) agenda	(C) deal	(D) paper			
Ans.	(C)						
Sol.	Normally, company signs a contract or deal, so use of 'deal' is proper here.						

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12.	What is your	_ for tonight?					
	(A) Principle	(B) Motto	(C) Plan	(D) Objective			
Ans.	(C)						
Sol.	The question give is more proper he		ormal routine of som	e special/specific day, so use of 'plan'			
13.	<b>Arrange the f</b>	ollowing sentences in correc	t pattern and mark a	t the correct combination. < /b>			
	1.Today we live i	n modern technology era.					
	P. We have a lot	of problems now.					
	Q. We want to ge	t everything in one day.					
	R. Ancient time w	vas quite pleasant.					
	S. We had no problems then.						
	C. Perhaps greed	I is the main cause for this.					
	(A) PQRS	(B) PRSQ	(C) SRQP	(D) RPQS			
Ans.	(B)						
Sol.	According to the events of sentence, PRSQ is best arrangement.						
14.	<b>Arrange the following sentences in correct pattern and mark at the correct combination.</b>						
	1.He is a commo	n man.					
	P. Yesterday our	city saw a brutal crime.					
	Q. Police is trying	to arrest innocent persons.					
	R. The criminals	are well known.					
	S. Police as well as whole system in corrupt.						
	C. Police will arrest him as he is an easy target because of being a common man.						
	(A) PQRS	(B) PRSQ	(C) QPRS	(D) PQSR			
Ans.	(A)						
Sol.	According to ever	nts of sentence, PRSQ is be	st arrangement.				
15.	<b>Arrange the following sentences in correct pattern and mark at the correct combination.</b>						
	1. I want to chang	ge the room.					
	P. Last month I g	ot a job.					
	Q. I had been livi	ng there for six months.					
	R. The office is far from the room.						
	S. I want to cut ex	penses of travelling.					
	C. Hopefully I will	do this next week.					
	(A) PQRS	(B) PRSQ	(C) QPRS	(D) PQSR			



Ans. (B)

Sol. Since, consecutive two letters are interchanged. Therefore,



Therefore, 64 will come in place of questions mark.

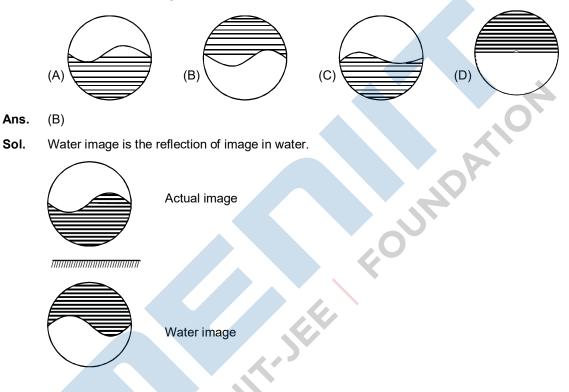
If '+' means '×', '-' means '+', '×' means '÷' and '÷' means '-', then
6 - 9 + 8 × 3 ÷ 20 =?
(A) -2
(B) 6
(C) 10
(D) 12

Ans. (C)

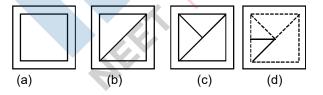
Sol. Interchanging the symbols as given in the above question, the above equation becomes

$$6 + 9 \times 8 \div 3 - 20 = 6 + 9 \times \frac{8}{3} - 20$$
$$= 6 + 24 - 20 = 10$$

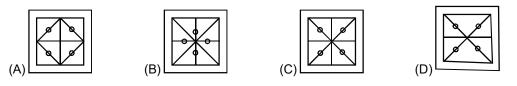
23. What is the water image of



24. A piece of paper is folded and penched as shown in the figure below



How will it appear when unfolded?



Ans. (B)

Sol.



On unfolding layer 2,

On unfolding layer 1,



On unfolding layer 3,



25. Here are some words translated from an artificial language.

mallon piml means blue light

mallon tifl means blue berry

arpan tifl means rasp berry

Which word could means 'light house'?

(A) tiflmallon (B) pimlarpan (C) mallonarpan

Ans. (D)

mallon piml = blue light mallon tifl = blue berry arpar(tifl)= rasp(berry)

Sol.

... From the above analysis, we see codes as

Blue = Mallon

Light = Piml

berry = tifl

rasp = arpan

:. Light i.e., piml is given in two option (b) and (d) but in option (b) other code given is of rasp, hence it cannot be the code of house. So, option (d) is correct.

(D) pimldoken

#### **BITSAT - 2014**

## MATHEMATICS

#### Single correct answer type

**1.** If p, q, r and s are positive real numbers such that p + q + r + s = 2, then M = (p + q) (r + s) satisfies the relation

(A) 0 < M ≤ 1

(C)  $2 \le M \le 3$ 

(D)  $3 \le M \le 4$ 

Ans. (A)

 $\textbf{Sol.} \qquad \text{Since, then } AM \geq GM \text{, then}$ 

$$\begin{split} & \frac{(p+q)+(r+s)}{2} \geq \sqrt{(p+q)(r+s)} \\ & \Rightarrow \frac{2}{2} \geq \sqrt{M} \Rightarrow \sqrt{M} \leq 1 \Rightarrow M \leq 1 \\ & \text{Also, } (p+q) \ (r+s) > 0 \quad (\ p,q,r,s>0) \\ & \therefore \ M > 0 \\ & \text{Hence,} 0 < M \leq 1 \end{split}$$

2. The complex number z = x + iy which satisfies the equation  $\left| \frac{z - 3i}{z + 3i} \right| = 1$ , lie on

(B)  $1 \le M \le 2$ 

(A) The X-axis

(B) The straight line y = 3

(C) A circle passing through origin (D) None of the above

Ans. (A)

Sol. Given,  $\left|\frac{z-3i}{z+3i}\right| = 1 \Rightarrow |z-3i| = |z+3i|$ (if  $|z_1-z_1| = |z-z_2|$ , then it is a perpendicular bisector of  $z_1$  and  $z_2$ )

Hence, perpendicular bisector of (0, 3) and (0, -3) is X-axis.

**3.** If (x) is an odd periodic function with period 2, then f(4) equal to

(A) -4 (B) 4 (C) 2 (D) 0

Ans. (D)

**Sol.** Since, f(x) is an odd periodic function with period 2.

$$\therefore \qquad f(-x) = -f(x) \text{ and } f(x+2) = f(x)$$

:. 
$$f(2) = f(0 + 2) = f(0)$$

and 
$$f(-2) = f(-2 + 2) = f(0)$$

Now, f(0) = f(-2) = -f(2) = -f(0)

$$\Rightarrow$$
 2f (0) = 0.i.e., f (0) = 0

:. f(4) = f(2 + 2) = f(2) = f(0) = 0

Thus, f (4) = 0

4. The solution of the differential equation

$$\frac{x + \frac{x^3}{3i} + \frac{x^5}{5!} + \dots}{1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \dots} = \frac{dx - dy}{dx + dy} \text{ is}$$
(A)  $2ye^{2x} = Ce^{2x} + 1$  (B)  $2ye^{2x} = Ce^{2x} - 1$  (C)  $ye^{2x} = Ce^{2x} + 2$  (D) None of these

Ans. (B)

Sol. We have, 
$$\frac{x + \frac{x^3}{3!} + \frac{x^5}{5!} + \cdots}{1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \cdots} = \frac{dx - dy}{dx + dy}$$

On applying componendo and dividend, we get

$$\frac{\left(x + \frac{x^3}{3i} + \frac{x^5}{5!} + \cdots\right) + \left(1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \cdots\right)}{\left(x + \frac{x^3}{3!} + \frac{x^5}{5!} + \cdots\right) - \left(1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \cdots\right)}$$

$$= \frac{\left(dx - dy\right) + \left(dx + dy\right)}{\left(dx - dy\right) - \left(dx + dy\right)}$$

$$\Rightarrow \frac{\left(1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \cdots\right)}{-\left(1 - x + \frac{x^2}{2!} - \frac{x^2}{3!} + \cdots\right)} = \frac{2dx}{-2dy}$$

$$\Rightarrow \frac{e^x}{-e^{-x}} = -\frac{dx}{dy}$$

$$\Rightarrow \frac{dy}{dx} = \frac{e^{-x}}{e^x} \Rightarrow \frac{dy}{dx} = e^{-2x} \Rightarrow dy = e^{-2x}dx$$

On integrating both sides, we get

$$y = \frac{e^{-2x}}{(-2)} + C_1 \Rightarrow 2y = -e^{-2x} + 2C_1$$
  
$$\Rightarrow 2y = -e^{-2x} + C \quad (where, C = 2C_1)$$
  
$$\Rightarrow 2ye^{2x} = -1 + e^{2x} C \Rightarrow 2ye^{2x} = Ce^{2x} - 1$$

- 5. The value of k such that the lines 2x 3y + k = 0, 3x 4y 13 = 0 and 8x 11y 33 = 0 are concurrent, is
  - (A) 20 (B) -7 (C) 7 (D) -20
- Ans. (B)
- Sol. Given lines are concurrent,

So, 
$$\begin{vmatrix} 2 & -3 & k \\ 3 & -4 & -13 \\ 8 & -11 & -33 \end{vmatrix} = 0$$
  
 $\Rightarrow 2(132 - 143) + 3(-99 + 104) + k(-33 + 32) = 0$   
 $\Rightarrow -22 + 15 - k = 0 \Rightarrow k = -7$   
6. Two lines, whose equations are  $\frac{x-3}{2} = \frac{y-2}{3} = \frac{z-1}{\lambda}$  and  $\frac{x-2}{3} = \frac{y-3}{2} = \frac{z-2}{3}$  lie in the same plane. Then, the value of is equal to sin sin  $\lambda$   
(A) 3 (B)  $\pi - 3$  (C) 4 (D)  $\pi - 4$   
Ans. (D)  
Sol. Given lines are  $\frac{x-3}{2} = \frac{y-2}{2} = \frac{z-1}{\lambda}$ .....(i)  
and  $\frac{x-2}{3} = \frac{y-3}{2} = \frac{z-2}{3}$ .....(ii)  
These lines lie in the same plane, So, both are coptanar.  
 $\therefore \begin{vmatrix} 2 & 3 & \lambda \\ 3 & 1 & 3 \\ 1 & -1 & -1 \end{vmatrix} = 0$   
 $\Rightarrow 2(-2 + 3) - 3(-3 - 3) + \lambda(-3 - 2) = 0$   
 $\Rightarrow 2 + 18 - 5\lambda = 0 \Rightarrow 5\lambda = 20 \Rightarrow \lambda = 4$   
 $\therefore$  sim<sup>-1</sup> sin  $\lambda = sin^{-1}sin 4$   
 $= sin^{-1}sin (\pi - 4)$   
 $= \pi - 4$   
7. If  $\frac{e^4}{1-x} = B_{\eta} + B_{\eta}x + B_{\eta}x^2 + \dots + B_{\eta}x^{\eta} + \dots$ , then the value of  $B_{\eta} - B_{\eta-1}$  is  
(A) 1 (B)  $\frac{1}{n}$  (C)  $\frac{1}{n!}$  (D) None of these  
Ans. (C)  
Sol. We have,  
 $e^{+} = (1 - x) (B_{\eta} + B_{\eta}x + B_{\eta}x^2 + \dots + B_{\eta}x^{n-1} + B_{\eta}x^{\eta} + \dots)$   
By the expansion of e<sup>\*</sup>, we get

Equating the coefficient of  $x^n$  on both sides, we get

 $B_n - B_{n-1} = \frac{1}{n!}$ 

## MENIIT

8. Z<sup>20</sup> - 7n - 1 is divisible by
(A) 64 (B) 36 (C) 49 (D) 25
Ans. (C)
Sol. Let P(n) = 2<sup>2n</sup> - 7n - 1 ⇒ P(1) = 0, P(2) = 49
P(1) and P(2) are divisible by 49.
Let P (k) = 2<sup>3n</sup> - 7k - 1 = 49 I
P (k + 1) = 2<sup>3k+3</sup> - 7k - 8
= 8(491 + 7k + 1) - 7k - 8
= 49(81) + 49k = 49λ.
(where, λ = 8I + k, which is an integer.)
9. If 
$$\int_{0}^{25} e^{x/4} dx = k(e^{-1})$$
, then the value of is k equal to
(A) 12 (B) 25 (C) 23 (D) 24
Ans. (B)
Sol. We know that, x, -[x] is periodic function with period one.
∴ e<sup>x+k1</sup>, has period one
Since, f (x) is periodic with period T, then f () f () f , - f , - f
 $\int_{0}^{17} f(x) dx = n \int_{0}^{1} f(x) dx$ 
 $25 \int_{0}^{16} e^{x/4} dx = 25 \int_{0}^{16} e^{x/4} dx$ 
 $25 \int_{0}^{16} e^{x/4} dx = 25 \int_{0}^{16} e^{x/4} dx$ 
10. A variable chool P C (1) = 1, k(e - 1)
Hence, k = 25
10. A variable chool P (0 of the parabola y2 = 4ax subtends a right angle at the vertex, then the locus of the point of intersection of the normal at P and Q is
(A) A parabola (B) A hyperbola (C) A circle (D) None of these
Ans. (A)
Sol. Let P be (al<sup>6</sup>, 2at,) and Q be (al<sup>6</sup>, 2at,). Since, PQ subtends a right angle at the vertex (0,0).

Hence,  $t_1t_2 = -4$  .... (i)

11.

12.

If (h, k) is the point of intersection of normal at P and Q, then

$$h_{(1)} = x_{1} \text{ is the point of the descendent of the matrix and c, users}$$

$$h_{-2} = a_{-1}(t_{1}^{2} + t_{2}^{2} + t_{1}(t_{2}) \dots (ii)$$
and  $k = -at_{1}t_{2}(t_{1} + t_{2}) \dots (iii)$ 
In order to find the locus of (h, k), we have to eliminate  $t_{1}$  and  $t_{2}$  between equations (i), (ii) and (iii),  

$$k = 4a_{-1}(t_{1} + t_{2}) \dots (iii)$$
If one equations (i) and (iii)]
and  $h_{-2}a = a_{-1}[(t_{1} + t_{2})]^{2} - t_{1}t_{2}$ 

$$\Rightarrow h_{-2}a = a_{-1}\left[\frac{k^{2}}{16a^{2}} + 4\right] \qquad \text{[from equation (iv)]}$$

$$\Rightarrow h_{-6}a = \frac{k^{2}}{16a^{2}}$$
Hence, the required locus is  $y^{2} = 16 a_{-1}(x - 6a)$ .
  
**11.** If  $\omega \neq 1$  is a cube root of unit, then
$$A = \begin{bmatrix} 1 + 2\omega^{100} + \omega^{200} & 0 \\ 1 & 1 + 2\omega^{100} & 0 \\ 0 & \omega^{2} & 2 + \omega^{100} + 2\omega^{200} \end{bmatrix}$$
(A) A is singular (B) |A|  $\neq 0$  (C) A is symmetric (D) None of the above
**Ans.** (A)
  
**Sol.** Given matrix can be rewritten as
$$A = \begin{bmatrix} 1 + 2\omega + \omega^{2} & \omega^{2} & 1 \\ 1 & 4 + \omega^{2} + 2\omega & 0 \\ 0 & \omega^{2} & 2 + \omega + 2\omega^{2} \end{bmatrix}$$
( $\because 1 + \omega + \omega^{2} = 0$ )
$$= \omega \begin{bmatrix} \omega & \omega & 1 \\ 0 & \omega & 0 \\ \omega & \omega^{2} & 1 + \omega^{2} \end{bmatrix}$$
( $\because 1 + \omega + \omega^{2} = 0$ )
  
**12.** 
$$\lim_{x \to a = 1} \frac{\tan^{2} x - 2 \tan x - 3}{\tan^{2} x - 4 \tan x + 3}$$
 equals to
(A) 1 (B) 2 (C) 0 (D) 3
  
**Ans.** (B)
  
**Sol.** 
$$\lim_{x \to a = 1} \frac{\tan^{2} x - 2 \tan x - 3}{\tan^{2} x - 4 \tan x + 3}$$

 $= \lim_{\tan x \to 3} \frac{(\tan x - 3)(\tan x + 1)}{(\tan x - 3)(\tan x + 1)}$  $= \lim_{\tan x \to 3} \frac{\tan x + 1}{\tan x - 1} = \frac{3 + 1}{3 - 1} = \frac{4}{3} = 2$ 

**13.** The locus of the points of intersection of the tangents at the extremities of the chords of the ellipse  $x^2 + 2y^2 = 6$  which touches the ellipse  $x^2 + 4y^2 = 4$ , is

(A)  $x^2 + y^2 = 4$  (B)  $x^2 + y^2 = 6$  (C)  $x^2 + y^2 = 9$  (D) None of these

Ans. (C)

Sol. The given equation of second ellipse can be rewritten as

$$\frac{x^2}{4}+\frac{y^2}{1}=1$$

Equation of tangent to this ellipse is

$$\frac{x}{2}\cos\theta + y\sin\theta = 1 \qquad \dots .(i)$$

Equation of the first ellipse can be rewritten as

$$\frac{x^2}{6} + \frac{y^2}{3} = 1$$
 .....(ii)

Let ellipse (i) meets the first ellipse at P and Q and the tangents at P and Q to the second ellipse intersected at (h, k), then equation (i) is the chord of contact of (h, k) with respect to the ellipse (ii) and thus, its equation is

$$\frac{hx}{6} + \frac{ky}{3} = 1 \qquad \qquad \dots \dots (iii)$$

Since, equations (i) and (iii) represent the same line

$$\frac{\frac{h}{6}}{\cos\frac{\theta}{2}} = \frac{\frac{ky}{3}}{\sin\theta} = 1$$

 $h=3\cos\theta$  and  $k=3\sin\theta$ 

Hence, locus is  $x^2 + y^2 = 9$ .

14. Number of roots of the equation  $|\sin x \cdot \cos x| + \sqrt{2 + \tan^2 x + \cot^2 x} = \sqrt{3}$ , where,  $x \in [0, 4\pi]$ , - are

Ans. (D)

**Sol.** We have, 
$$|\sin x \cos x| + |\tan x + \cot x| = \sqrt{3}$$
,

$$\Rightarrow \left|\sin x \cos x\right| + \frac{1}{\left|\sin x \cdot \cos x\right|} = \sqrt{3}$$

But 
$$|\sin x \cdot \cos x| + \frac{1}{|\sin x \cdot \cos x|} \ge 2$$

Hence, there is no solution.

**15.** If 
$$(f(x) = \begin{cases} \left[ tan\left(\frac{\pi}{4} + x\right) \right]^{\frac{1}{x}} & x \neq 0 \\ k, & x = 0 \end{cases}$$

For what value of 'k' f(x) is continuous at x = 0?

(A) 1 (B) 0 (C) e (D) 
$$e^2$$
  
Ans. (D)  
Sol.  $\lim_{x\to 0} \left[ \tan\left(\frac{\pi}{4} + X\right) \right]^{\frac{1}{x}} = \lim_{x\to 0} \left[ \frac{1 + \tan x}{\tan - \tan x} \right]^{\frac{1}{x}}$   
 $= \lim_{x\to 0} \left[ (1 + \tan x)^{\frac{1}{\tan x}} \right]^{\frac{1}{x}} \times \lim_{x\to 0} \left[ (1 - \tan x)^{\frac{1}{\tan x}} \right]^{\frac{1}{x}}$   
 $= e \times e = e^2$   
16. The period of  $\sin^2 \theta$  is  
(A)  $\pi^2$  (B)  $\pi$  (C)  $2\pi$  (D)  $\frac{\pi}{2}$   
Ans. (B)  
Sol. Since,  $\sin^2 \theta = \frac{1 - \cos \theta}{2} = \frac{1}{2} - \frac{1}{2} \cos 2\theta$   
 $\therefore$  Period of  $\sin^2 \theta = \frac{2\pi}{2} = \pi$ 

**17.** Five persons, A, B, C, D and E are in queue of a shop. The probability that and A are E always together, is

(A) 
$$\frac{1}{4}$$
 (B)  $\frac{2}{3}$  (C)  $\frac{2}{5}$  (D)  $\frac{3}{5}$ 

Ans. (C)

Sol. ∴ Total number of ways = 5! and favourable number of ways = 2 × 4!

$$\therefore \text{ Required probability } = \frac{2 \times 4!}{5!} = \frac{2}{5}$$

18. 
$$\lim_{x \to \infty} \frac{x^4 \cdot \sin\left(\frac{1}{x}\right) + x^2}{1 + |x|^3} \text{ equal to}$$
(A) 0 (B) -1 (C) 2 (D) 1  
Ans. (B)  
Sol. 
$$\lim_{x \to \infty} \frac{x^4 \cdot \sin\left[\frac{1}{x}\right] + x^2}{1 + |x|^3} = \lim_{x \to \infty} \left[\frac{x \sin\left(\frac{1}{x}\right) + \frac{1}{x}}{\frac{1}{x^3} + \frac{|x|^3}{x^3}}\right]$$
[Dividing numerator and denominator by x<sup>3</sup>]  

$$= \frac{\lim_{x \to \infty} \frac{1}{\frac{1}{x}} + \lim_{x \to \infty} \frac{1}{x^3}}{\lim_{x \to \infty} \frac{1}{x^3}} = \frac{1 - 0}{0 - 1} = -1$$
19. The sum of the log<sub>4</sub> 2 - log<sub>8</sub> 2 + log<sub>16</sub> 2 ... ls  
(A) e<sup>2</sup> (B) log<sub>8</sub> 2 + 1 (C) log<sub>8</sub> 3 - 2 (D) 1 - log<sub>8</sub> 2  
Ans. (D)  
Sol Given that, log<sub>4</sub> 2 - log<sub>8</sub> 2 + log<sub>16</sub> 2 -...  

$$= \frac{1}{\log_2 4} - \frac{1}{\log_2 8} + \frac{1}{\log_2 16} - \cdots$$

$$= \frac{1}{2} - \frac{1}{3} + \frac{1}{4} - \cdots$$

$$= 1 - \left[1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \frac{1}{5} - \cdots\right]$$

$$= 1 - \log_8 2$$

**20.** The mean of n terms is  $\overline{\mathbf{x}}$ . If the first term is increased by 1, second by 2 and so on, then the new mean is

(A) 
$$\overline{x} + n$$
 (B)  $\overline{x} + \frac{n}{2}$  (C)  $\overline{x} + \frac{n+1}{2}$  (D) None of these

Ans. (C)

 $\textbf{Sol.} \qquad \text{Let the observation be } x_1, \, x_2.x_3 \, \dots , \, x_n.$ 

Now, mean  $(\overline{\mathbf{x}}) = \frac{\mathbf{x}_1, \mathbf{x}_2 + \dots + \mathbf{x}_n}{n}$ 

When first term increased by 1, second by 2 and so on, then observations will be

 $(x_1 + 1), (x_1 + 2), (x_1 + 3), \dots, (x_n + n)$ 

Then, new mean

$$\begin{aligned} &(\bar{x}_{1}) = \frac{(x_{1}+1)+(x_{2}+2)+\dots+n}{n} \\ &= \frac{(x_{1}+x_{2}+\dots+x_{n})+(1+2+3+\dots+n)}{n} \\ &\Rightarrow \qquad \bar{x}_{1} = \frac{x_{1}+x_{2}+\dots+x_{n}}{n} + \frac{1+2+3+\dots+n}{n} \\ &\Rightarrow \qquad \bar{x}_{1} = \bar{x} + \frac{n(n+1)}{2n} \qquad \left[ \because \qquad 1+2+3+\dots+n = \frac{n(n+1)}{2} \right] \\ &\Rightarrow \qquad \bar{x}_{1} = \bar{x} + \frac{n+1}{2} \end{aligned}$$

21. The greatest and least values of  $(\sin^{-1}x)^2 + (\cos^{-1}x)^2$  are respectively

The greatest and least values of 
$$(\sin^{-1}x)^2 + (\cos^{-1}x)^2$$
 are respectively  
(A)  $\frac{\pi^2}{4}$  and 0 (B)  $\frac{\pi}{2}$  and  $\frac{-\pi}{2}$  (C)  $\frac{5\pi^2}{4}$  and  $\frac{\pi^2}{8}$  (D)  $\frac{\pi^2}{4}$  and  $\frac{-\pi^2}{4}$   
(C)  
We have,  
 $(\sin^{-1}x)^2 + (\cos^{-1}x)^2$   
 $= (\sin^{-1}x + \cos^{-1}x)^2 - 2\sin^{-1}x \times \cos^{-1}x$   
 $= \frac{\pi^2}{4} - 2\sin^{-1}x \left(\frac{\pi}{2} - \sin^{-1}x\right)^2$   
 $= 2\left[(\sin^{-1}x)^2 - \frac{\pi}{2}\sin^{-1}x + \frac{\pi^2}{8}\right]$ 

Ans. (C)

Sol. We have,  

$$(\sin^{-1}x)^{2} + (\cos^{-1}x)^{2}$$

$$= (\sin^{-1}x + \cos^{-1}x)^{2} - 2\sin^{-1}x \times \cos^{-1}x$$

$$= \frac{\pi^{2}}{4} - 2\sin^{-1}x \left(\frac{\pi}{2} - \sin^{-1}x\right)$$

$$= \frac{\pi^{2}}{4} - \pi\sin^{-1}x + 2(\sin^{-1}x)^{2}$$

$$= 2\left[\left(\sin^{-1}x\right)^{2} - \frac{\pi}{2}\sin^{-1}x + \frac{\pi^{2}}{8}\right]$$

$$= 2\left[\left(\sin^{-1}x - \frac{\pi}{4}\right)^{2} + \frac{\pi^{2}}{16}\right]$$

Thus, the least value is  $2\left(\frac{\pi^2}{16}\right)$  i.e.,  $\frac{\pi^2}{8}$  and the greatest value is  $2\left[\left(\frac{-\pi}{2}-\frac{\pi}{4}\right)^2+\frac{\pi^2}{16}\right]$  i.e.,  $\frac{5\pi^2}{4}$ .

22. The probability of simultaneous occurrence of atleast one of two events A and B is p. If the probability that exactly one of A, B occurs is q, then p (A') + P (B') is equal to

(A) 
$$2 - 2p + q$$
 (B)  $2 + 2p - q$  (C)  $3 - 3p + q$  (D)  $2 - 4p + q$ 

- Ans. (A)
- Sol. Since, P (exactly one of A, B occurs) = q (given), We get

	$P(A \cup B) - P(A \cap B) = q$						
	$\Rightarrow$	p – P (A ∩ B) :	= q				
	$\Rightarrow$ P (A $\cap$ B) = p = q						
	$\Rightarrow$ 1 – P (A' $\cup$ B') = p – q						
		P (A' ∪ B') = 1					
			- P (A' ∩ B') = 1 + q – p				
			= (1 + q + p) + [1 – P (A	(JB)]			
		(1 – P + q) + (					
	=	2 – 2p +q	.,		•		
23.			erential equation $x = 1 + \frac{1}{2}$				
	(A) y =	log x + C	(B) $y^2 = (\log x)^2 + C$	(C) $y = \log x + xy$	(D) $xy = x^y + C$		
Ans.	(B)						
Sol.	The gi	ven equation is	reduced to $\mathbf{x} = \mathbf{e}^{xy\left(\frac{dy}{dx}\right)}$		A		
	$\Rightarrow$	$\log x = xy \frac{dy}{dx}$		<u>نې کې ا</u>	0		
	$\Rightarrow$	$y dx = \frac{\log x}{x} dx$					
	$\Rightarrow$	$\int y  dx = \int \frac{1}{x} \log x$	xdx				
	⇒	$\frac{y^2}{2} = \frac{\left(\log x\right)^2}{2}$	+ C'				
	$\Rightarrow$	$y^2 = (\log x)^2 +$	2C'				
	⇒	$y^2 = (\log x)^2 +$	с	(where, C = 2C')			
24.	If n is a	a positive intege	r, then n³ + 2n is divisible	e by			
	(A) 2		(B) 6	(C) 15	(D) 3		
Ans.	(D)						
Sol.		$(n) = n^3 + 2n$					
	. ,	= 1 + 2 = 3					
	. ,	8 + 4 = 12					
	. ,	= 27 + 6 = 33					
25			I these numbers are divis	-	pritivo intogen is		
25.	(A) 0		ients in the expansion of (B) n	(C) 1	(D) –1		
	(,,)0						

Ans.	(C)						
Sol.	∵ Using Binomial theorem,						
	$(5x - 4y)^n = {}^nC_o(5x)^n +$	${}^{n}C_{1}(5x)^{n-1}(-4y) + {}^{n}C_{2}(5x)^{n-1}(-4y) + {}^{n}C_{2}(5x$	$(-4y)^{n-2} (-4y)^2 + + {}^{n}C_{n}(-4y)^{n-2} (-4y)^{n-2} ($	y) <sup>n</sup>			
	Sum of coefficients						
	$= {}^{n}C_{o}5^{n} + {}^{n}C_{1} 5^{n-1}(-4)$	+ ${}^{n}C_{2}5^{n-2}$ . (-4) <sup>2</sup> + + ${}^{n}C_{2}5^{n-2}$	C <sub>n</sub> (-4) <sup>n</sup>				
	$= (5-4)^n$						
	= 1 <sup>n</sup> = 1						
26.	The distance of the po	int (1,–5,9) from the plar	ne x + y + z = 5 measure	d along a straight line x = y = z is			
	$2\sqrt{3}$ k, then the value of	of is					
	(A) 5	(B) 6	(C) √3	(D) 4			
Ans.	(A)						
Sol.	Given equation of plar	ne is x + y + z = 5					
	The distance measure	d along the line x = y = z	<u>.</u>				
	Direction ratio's of the	given line is (1, 1, 1).		0			
	So, the equation of line	e PQ is					
	$\frac{x-1}{1} = \frac{y+5}{1} = \frac{z-9}{1}$			Or			
	Now, let $\frac{x-1}{1} = \frac{y+5}{1} = \frac{z-9}{1} = \lambda$						
	$x = \lambda + 1, y = \lambda - 5, z = \lambda + 9$						
	Lies on the plane x + y	/ + z = 5					
	$\lambda + 1 - \lambda + 5 + \lambda + 9 =$	5					
	$\Rightarrow$ $\lambda = -10$						
	The coordinate of Q is	(-99, -15, -1) and the c	coordinate of P is (1, –5,§	9).			
	$PQ = \sqrt{(10)^2 + (10)^2 + (10)^2}$	$(10)^2 = 10\sqrt{3}$					
	PQ = $\sqrt{(10)^2 + (10)^2 +}$ ∴ $2\sqrt{3}k = 10\sqrt{3}$	$\Rightarrow$ k = 5					
27.	$\lim_{x\to 1} \frac{x^m - 1}{x^n - 1}$ is equal to						
	(A) $\frac{n}{m}$	(B) <u>m</u>	(C) $\frac{2m}{n}$	(D) 2n/m			
Ans.	(B)						
Sol.	$\lim_{x \to 1} \frac{x^m - 1}{x^n - 1} = \lim_{x \to 1} \frac{mx^{m-1}}{nx^{n-1}}$	(by L' Hospital rule)					

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 $=rac{m}{n}$ 

28. The value of x > 1 satisfying the equation 
$$\int_{1}^{x} t \log t dt = \frac{1}{4}$$
, is  
(A)  $\sqrt{e}$  (B)  $e^{\frac{3}{2}}$  (C)  $e^{2}$  (D)  $2e - 1$   
Ans. (A)  
Sol. Consider that,  $I = \int_{1}^{x} t \log t dt$   
 $= \left[ \log t, \frac{t^{2}}{2} \right]_{1}^{x} - \frac{1}{2} \left[ \frac{t^{2}}{2} \right]_{1}^{x}$   
 $= \frac{x^{2}}{2} \log x - \frac{1}{2} \left[ \frac{t^{2}}{2} \right]_{1}^{x}$   
 $= \frac{x^{2}}{2} \log x - \frac{1}{2} \left[ \frac{x^{2}}{2} - \frac{1}{2} \right]$   
 $\Rightarrow \frac{1}{4} = \frac{x^{2}}{1} \log x - \frac{1}{4} (x^{2} - 1)$   
 $\Rightarrow \frac{1}{2}x^{2} \log x - \frac{1}{4}x^{2} = 0$  (as x > 1)  
 $\Rightarrow x^{2}(2 \log x - 1) = 0$   
 $\Rightarrow 2 \log x - 1 = 0$   
 $\Rightarrow \log x = \frac{1}{2}$   
 $\Rightarrow x = e^{\frac{1}{2}}$   
 $\Rightarrow x = \sqrt{e}$   
29.  $a = \sum_{n=0}^{\infty} \frac{x^{2n}}{3n!} b = \sum_{n=1}^{\infty} \frac{x^{2n-2}}{(3n-2)!} And c = \sum_{n=1}^{\infty} \frac{x^{2n-1}}{(3n-1)!}$  then the value of  $a^{3} + b^{3} + c^{3} - 3abc$  is  
(A) 1 (B) 0 (C) -1 (D) -2  
Ans. (A)  
Sol.

We have,

$$a = \sum_{n=0}^{\infty} \frac{x^{3n}}{3n!}, b = \sum_{n=1}^{\infty} \frac{x^{3n-2}}{(3n-2)!} \text{ and } c = \sum_{n=1}^{\infty} \frac{x^{3n-1}}{(3n-1)!'}$$

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Now, 
$$a+b+c = \sum_{n=1}^{\infty} \frac{x^{2n}}{3n!} b = \sum_{n=1}^{\infty} \frac{x^{2n-2}}{(3n-2)!} And c = \sum_{n=1}^{\infty} \frac{x^{2n}-1}{(3n-1)}$$
  
=  $1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots = e^x$   
 $a+bw+cw^2 = 1 + \omega x = \frac{\omega^2 x^2}{2!} + \frac{\omega^3 x^3}{3!} + \dots = e^{wx}$   
and  $a+bw^2 = cw = e^{w^2x}$ ,  $\omega$  is imaginary cube root of unity.  
Now,  $a^3 + b^3 + c^3 - 3abc$   
=  $(a+b+c)(a+bw+cw^2)(a+bw^2+cw)$   
 $e^x$ ,  $e^{w^2}, e^{w^2}, e^{w^2} = e^{1(a+w^2)} = e^{ax} = 1$   
30. The unit vector perpendicular to the vectors  $\hat{1} - \hat{1}$  and  $\hat{1} + \hat{1}$  forming a right handed system is  
(A)  $\hat{k}$  (B)  $-\hat{k}$  (C)  $\frac{\hat{1} - \hat{1}}{\sqrt{2}}$  (D)  $\frac{\hat{1} + \hat{1}}{\sqrt{2}}$   
Ans. (A)  
Sol. Required unit vector is  $\frac{(\hat{1} - \hat{1}) \times (\hat{1} + \hat{1})}{|(\hat{1} - \hat{1}) \times (\hat{1} + \hat{1})|}$   
31. The number of solutions of the equation in  $x^2 + 2x^2 + 5x + 2\cos x = 0$  in [0,2n] are  
(A) 0 (B) 1 (C) 2 (D) 3  
Ans. (A)  
Sol. f(x) =  $x^3 + 2x^2 + 5x + 2\cos x$   
 $f(x) = 3x^2 + 4x + 5 - 2 \sin x$   
 $\Rightarrow f(x) > 0, \forall x$   
 $f(x)$  is increasing for all  $x \in \mathbb{R}$ .  
Also, f(0) =  $2 \Rightarrow f(x) = 0$   
So, f(x) has no solution:  
32.  $\lim_{x\to 0} \frac{(1+x)^3 - 1}{(1+x)^2 - 1}$  is equal to  
(A) 8 (B) 6 (C) 4 (D) 2  
Ans. (C)  
Sol.  $\lim_{x\to 0} \frac{(1+x)^3 - 1}{(1+x)^2 - 1}$ 

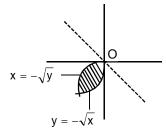
$$= \lim_{x \to 0} \frac{\left[ (1+x)^4 + 1 \right] \left[ (1+x)^2 \right] \left[ (1+x)^2 - 1 \right]}{(1+x)^2 - 1}$$
  
= 2 × 2 = 4

**33.** The area bounded by the curves  $y = -\sqrt{-x}$  and  $x = -\sqrt{-y}$ , where x,  $y \le 0$ , where, is

(A) 
$$\frac{1}{3}$$
 (B)  $\frac{1}{4}$  (C)  $\frac{1}{5}$  (D)  $\frac{1}{2}$ 

Ans. (A)

**Sol.** Given that,  $y = -\sqrt{-x}$ 



 $\Rightarrow$  y<sup>2</sup> = -x, where x and y both negative.

Now, 
$$y = -\sqrt{-x}$$

 $\Rightarrow$  y<sup>2</sup> = -x, where x and y both negative.

$$\therefore \qquad \text{Area} = \left| \int_{-1}^{0} -\sqrt{-x} \, dx - \int_{-1}^{0} -x^2 \, dx \right|$$
$$= \frac{1}{3}$$

**34.** If a and b are the roots of the equation  $x^2 - px + q$ , then the value of  $(\alpha + \beta)x - \beta = 0$ 

$$\left(\frac{\alpha^2+\beta^2}{2}\right)x^2+\left(\frac{\alpha^2+\beta^2}{3}\right)x^3+\cdots$$
, is

(A)  $\log(1 - px + qx^2)$  (B)  $\log(1 + px - qx^2)$  (C)  $\log(1 + px + qx^2)$  (D) None of these (A)

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Ans. (A

**Sol.** Given series 
$$\left[\alpha x - \frac{1}{2}(\alpha x)^2 + \frac{1}{3}(\alpha x)^3 - \cdots\right] + \left[\beta x - \frac{1}{2}(\beta x)^2 + \frac{1}{3}(\beta x)^3 - \cdots\right]$$

= log 
$$(1 - ax)$$
 + log  $(1 - \beta x)$   
= log  $[1 - (\alpha + \beta) x + \alpha \beta x^2]$   
Now,  $\alpha + \beta$  = p and  $\alpha\beta$  = q

Given series = log  $(1 - px + qx^2)$ 

35.

(D) x > 0

If  $\cos^{-1} x > \sin^{-1} x$ , then (A)  $\frac{1}{\sqrt{2}} < x \le 1$  (B)  $0 \le x < \frac{1}{\sqrt{2}}$  (C)  $-1 \le x < \frac{1}{\sqrt{2}}$ Ans. (C) Sol. We know that,  $\sin^{-1} x + \cos^{-1} x = \frac{\pi}{2}, \forall x \in \left[-1, 1\right]$  $\therefore \cos -1 x > \sin -1 x$  $\Rightarrow \frac{\pi}{2} - \sin^{-1} x > \sin^{-1} x$  $\Rightarrow \frac{\pi}{2} > 2 \sin - 1x$  $\Rightarrow$  sin-1x <  $\frac{\pi}{4}$  $\Rightarrow x < \frac{1}{\sqrt{2}}$  $\therefore$   $-1 \le x < \frac{1}{\sqrt{2}}$ 

A student is allowed to select atmost books from a collection of (2n + 1) books. If the number of ways in 36. which he can do this, is 64, then the value of is

(A) 6 (B) n (C) 3 (D) None of these

- Ans. (C)
- Sol. Number of ways

 $= =^{2n+1} \mathbf{C}_0 +^{2n+1} \mathbf{C}_1 +^{2n+1} \mathbf{C}_2 + \dots +^{2n+1} \mathbf{C}_2$ 

$$=\frac{1}{2}(2^{2n+1})=2^{2n+1}$$

Thus, 2<sup>2n</sup> = 64

i.e., 2<sup>2n</sup> = 64

On comparing,  $2n = 6 \Rightarrow n = 3$ 

- 37. Let R = (3,3) (6, 6) (9, 9) (12, 12) (6, 12) (3, 9) (3, 12) (3,6) () + be a relation on the set A = {3, 6, 9, 12}. The relation is
  - (A) An equivalence relation
  - (C) Reflexive and transitive

- (B) Reflexive and symmetric
- (D) Only reflexive

Ans. (C) MENIIT

R is reflexive as (3, 3), (6, 6), (9, 9), (12, 12) ∈ R.R is not symmetric as (6, 12) ∈ R but (12, 6) ∉ R.R is Sol. transitive as the only pair which needs verification is (3, 6) and  $(6, 12) \in R$  $\Rightarrow$ (3, 12) ∈ R. 38. The value of a, so that the sum of squares of the roots of the equation  $x^2 - (a - 2)x - a + = 0$  assume the least value, is (A) 2 (B) 0 (C) 3 (D) 1 Ans. (D) Sol. Let  $\alpha$  and  $\beta$  be the roots of the equation  $x^{2} - (a - 2)x - a + 1 = 0$  $\therefore \alpha + \beta = a - 2 \text{ and } \alpha\beta = -(a - 1)$  $s = \alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta = (a - 2)^2 + 2(a - 1)$  $= a^{2} - 4a + 4 + 2a - 2 = a^{2} - 2a + 2$ Now,  $\frac{ds}{da} = 2a - 2$ OUNDATIS For maximum and minimum,  $\frac{ds}{da} = 0$ 2a - 2 = 0 $\Rightarrow$  $\Rightarrow$ a = 1  $\frac{d^2s}{da^2} = 2 > 0$ Also, Hence, at a = 1, s will have minimum value. The form of the differential equation of the central conics is 39. (A)  $x = y \frac{dy}{dx}$  $x^2 + xy \frac{d^2y}{dx^2} - y \frac{dy}{dx} = 0$  $(C) x + y \frac{d^2 y}{dx^2} = 0$ (D) None of the above

Ans. (D)

**Sol.** We have,  $ax^2 + by^2 = 1$ 

On differentiating both sides w.r.t. , we get

$$2ax + 2by \frac{dy}{dx} = 0$$
  

$$\Rightarrow ax + by \frac{dy}{dx} = 0 \qquad \dots \dots (i)$$
  

$$\Rightarrow \qquad \frac{-a}{b} = \frac{y}{x} \frac{dy}{dx} = 0 \qquad \dots \dots (ii)$$

Again, differentiating equation (i) w.r.t x, we get

$$a + b\left(\frac{dy}{dx}\right)^{2} + by\frac{d^{2}y}{dx^{2}} = 0$$
$$\Rightarrow -\frac{a}{b} = \left(\frac{dy}{dx}\right)^{2} + y\frac{d^{2}y}{dx^{2}} \quad \dots \dots (iii)$$

From equations (ii) and (iii), we get ]

$$\frac{y}{x}\frac{dy}{dx} = \left(\frac{dy}{dx}\right)^2 + y\frac{d^2y}{dx^2}$$
$$\Rightarrow \left(\frac{dy}{dx}\right) = x\left(\frac{dy}{dx}\right)^2 + xy\frac{d^2y}{dx^2}$$

- 40. A furniture dealer deals in only two items namely tables and chairs. He has Rs. 5000 to invest and space to store at the most 60 pieces. A table cost him rs 250 and a chair rs 60. He can sell a table at a profit of rs 15. Assume that the can sell all the items that he produced. The number of constraints in the problem are
- (A) 2 (C) 4 (B) 3 Ans. (C) FOUNE
- Sol. If x tables and y chairs are purchased for maximum profit.

Then,  $x + y \le 60$ 

$$5x + \frac{6y}{5} \le 100$$

$$x \ge 0, y \ge 0$$

So, number of constraints are four.

- 41.  $10^{n} + 3 (4^{n+2}) + 5$  is divisible by  $(n \in N)$ (B) 5
  - (A) 7

(C) 9

(D) 17

- (C) Ans.
- For n =1, 10<sup>n</sup> + 3 ×4<sup>3</sup> + 5 Sol. = 207, which is divisible by 99 So, by induction, the result is divisible by 9.
- 42. The total number of subsets of a finite set A has 56 more elements than the total number of subsets of another finite set B. What is the number of elements in the set A?
  - (A) 5 (B) 6 (C) 7 (D) 8
- Ans. (B)
- Sol. Let set A and B have m and n elements, respectively.

 $2^{m} - 2^{n} = 56$  $2^{n} (2^{m-n} - 1) = 56 = 8 \times 7 = 2^{3} \times 7$ Comparing both sides, we get  $2^{n} = 2^{3}$  and  $2^{m-n} = 7$  $n = 3 \text{ and } 2^{m-n} = 8$  $2^{m-n} = 2^3 \Longrightarrow m - n = 3$  $\Rightarrow$  m – 3 = 3  $\Rightarrow$  m = 6

Number of the elements in A is 6.

43. A sample of 35 observation has the mean 80 and standard deviation as 4. A second sample of 65 observations from the same population has mean 70 and standard deviation 3. Then, the standard deviation of the combined sample is

(A) 5.85

(C) 34.2

(D) None of the above

Ans. (A)

Sol. Mean of the combined sample

$$\overline{\mathbf{x}} = \frac{\mathbf{n}_1 \overline{\mathbf{x}}_1 + \mathbf{n}_2 \overline{\mathbf{x}}_2}{\mathbf{n}_1 + \mathbf{n}_2} = \frac{35 \times 80 + 65 \times 70}{35 + 65}$$

= 73.5

FOUNDATH Standard deviation of the combined sample is given by

(B) 5.58

$$\sigma^{2} = \frac{n_{1}(\sigma_{1}^{2} + d_{1}^{2}) + n_{2}(\sigma_{2}^{2} + d_{2}^{2})}{n_{1} + n_{2}}$$

Where,  $d_1^2 = (\overline{x}_1 - \overline{x})^2 = (80 - 73.5)^2 = 42.25$ 

$$d_2^2 = (\overline{x}_2 - \overline{x})^2 = (70 - 73.5)^2 = 12.25$$

$$\sigma^{2} = \frac{35(4^{2} + 42.25) + 65(3^{2} + 12.25)}{35 + 65}$$

σ  $= 34.2 \Rightarrow \sigma = 5.85$ 

44. Three straight lines 2x + 11y - 5 = 0, 24x + 7y - 20 = 0 and 4x - 3y - 2 = 0

- (A) From a triangle
- (B) Are only concurrent

(C) Are concurrent with one line bisecting the angle between the other two

- (D) None of the above
- Ans. (C)

Sol. For the two lines 24x + 7y - 20 = 0 and 4x - 3y - 2 = 0, the angle bisectors are given by

$$\frac{24x+7y-20}{25} = \pm \frac{4x-3y-2}{5}$$

Taking positive sign, we get 2x + 11y - 5 = 0

So, the given three lines are concurrent with one line bisecting the angle between the other two.

45. If the plane x + y + z = 1 is rotated through an angle 90° about its line of intersection with the plane x - z = 12y + 3z = 0, then the now position of the plane is

(A) x - 5y + 4y = 1(B) x - 5y + 4z = -1(C) x - 8y + 7z = 2 (D) x - 8y + 7 - 2

Ans. (D)

Sol. The new position of plane is

$$(x - 2y + 33) + \lambda (x + y + z - 1) = 0$$

 $(1 + \lambda) x + (\lambda - 2) y + (3 + \lambda) z - \lambda = 0$  $\Rightarrow$ 

Given that this is perpendicular to x + y + z = 1

- $(1 + \lambda) \times 1 + (\lambda 2) \times 1 + (3 + \lambda) \times 1 = 0$ *:*..
- $1 + \lambda + \lambda \Box 2 + 3 + \lambda = 0$  $\Rightarrow$
- $3\lambda + 2 = 0$  $\Rightarrow$

$$\Rightarrow \qquad \lambda = \frac{-2}{3}$$

Hence, the new position of the plane is  $(x - 2y + 3z) - \frac{2}{3}(x + y + z - 1) = 0$ 

$$\Rightarrow 3x - 2x - 6y - 2y + 9z - 2z + 2 = 0$$
$$x - 8y + 7z = -2$$

$$x - 8y + 7z = -2$$

ΔΔ

## PHYSICS

## Single correct answer type

**1.** In process of amplitude modulation of signal to be transmitted.

Signal to be modulated is given by  $m(t) = A_m \sin \omega_m t$ , carrier wave is given by  $c(t) = A_c \sin \omega_c t$ , modulated signal  $c_m(t)$  is given by

(A)  $C_m$  (t) =  $A_c \sin \omega_c t + A_m \sin \omega_m t$ 

(C)  $C_m(t) = [A_c m(t) \sin \omega_c t]$ 

(B)  $C_m$  (t) = ( $A_c + A_m$ ) sin  $\omega_c$  t

e h

(D) None of the above

Ans. (C)

Ans. Sol.

Sol. In amplitude modulation, amplitude of carrier wave varies with signal to be modulated so modulated signal C<sub>m</sub>(t) is given by

 $C_m(t) = [A_c + m(t)] \sin \omega_c t$ 

 $\Rightarrow$   $C_m(t) = (A_c + A_m \sin \omega_m t) \sin \omega_c t$ 

As  $m(t) = A_m \sin \omega_m t$  (given)

2. Graph of stopping potential for most energetic emitted photoelectron (V<sub>s</sub>) with frequency of incident radiation on metal is given below

Value of 
$$\frac{AB}{BC}$$
, in graph is  
 $V_s \oint_{0} \oint_{V_0} f_{0} f_{0} f_{0}$   
(h = Planck's constant, e – electronic charge)  
(A) h (B) e (C)  $\frac{h}{e}$  (D)  
(C)  
By Einstein's photoelectric effect equation  
 $KE_{max} = eV_s = hv - hv_0$   
 $\Rightarrow V_s = (\frac{h}{e})v - \frac{hv_0}{e}$   
Graph of Vs with v is straight line whose slope  $\frac{h}{e}$ 

From given graph slope  $= \frac{AB}{BC} \Rightarrow \frac{AB}{BC} = \frac{h}{e}$ 

3. A block of mass 0.18 kg is attached to a spring of force constant 2 N/m. The coefficient of friction between the block and the floor is 0.1. Initially the block is at rest and the spring is unstretched. An impulse is given to the block.

The block slides a distance of 0.06m and comes to rest for the first time the initial velocity of the block in m/s is v = N/10. Then N is

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(A) 2 (B) 2 (C) 4 (D) 6

Ans. (C)

**Sol.** Here, m = 0.18 kg, K = 2 N/m,  $\mu = 0.1$ , x = 0.06m.

According to conservation of mechanical energy principle, we know

Decrease in mechanical energy = Work done against friction

$$\frac{1}{2}mv^{2} - \frac{1}{2}kx^{2} = \mu mgx$$
$$\Rightarrow v = \sqrt{\frac{2\mu mgx + Kx^{2}}{m}}$$

Substituting the values of m,  $\mu$ , g, x and K, we get

$$v = \sqrt{\frac{2 \times 0.1 \times 0.18 \times 9.8 \times 0.06 + 2 \times 0.066}{0.18}}$$

$$v = \left(\frac{4}{10}\right) m / s$$

So, N = 4

4. Ohm's law says

(A) V = IR

(B) V/I = constant

(C) Both (V = IR) and (V/I = constant) are correct

(D) Both (V = IR) and (V/I = constant) are incorrect

Ans. (B)

Sol. Ohm's law says

 $\frac{V}{I} = R = constant$ 

**5.** A train accelerating uniformly from rest attains a maximum speed of 40 ms<sup>-1</sup> in 20s. It travels at this speed for 20s and is brought to rest with uniform retardation in further 40s. What is the average velocity during this period?

```
(A) 80m/s (B) 25 m/s (C) 40 m/s (D) 30 m/s
```

Ans. (B)

**Sol.** (i) v = u + at<sub>1</sub>

 $40 = 0 + a \times 20$ ∴ a = m/s<sup>2</sup>  $v^2 - u^2 = 2as$  $40^2 - 0 = 2 \times 2s_1$ ∴ s<sub>1</sub> = 400 m (ii)  $s_2 = v \times t_2 = 40 \times 20 = 800 \text{ m}$ (iii) v = u + at= 0 = 40 + a × 40  $a = -1 \text{ m/s}^2$ *.*..  $02 - 40^2 = 2(-1) s_3$ s<sub>3</sub> = 800 m ÷. Total distance travelled  $= s_1 + s_2 + s_3$ = 400 + 800 + 800 = 2000 m Total time taken = 20 + 40 = 80 s  $\therefore$  Average velocity =  $\frac{2000}{80}$  = 25 m / s

6. The strain-stress curves of three wires of different material are shown in the figure. P, Q, R are the elastic limits of the wires, the figure shows that

(A) Elasticity of wire P is maximum

- (C) Tensile strength of R is maximum
- (B) Elasticity of wire Q is maximum

(D) None of the above

- Ans. (C)
- **Sol.** As stress is shown on -axis and strain on -axis.

So, we can say that  $y = \cot \theta = \frac{1}{\tan \theta} = \frac{1}{\text{slope}}$ 

So, elasticity of wire P is minimum and R is maximum.

- 7. For the equation  $F \propto A^a v^b d^c$ , where F is the force, A is the area, v vis the velocity and d is the density, the values of a, b and c are respectively.
  - (A) 1, 2, 1 (B) 2, 1, 1 (C) 1, 1, 2 (D) 0, 1, 1

Ans. (A) Sol.  $[MLT-2] = [L^{2a}] \times [L^{b} T^{-b}] [M^{c} L^{-3c}]$ = [M<sup>c</sup> L<sup>2a + b -3c</sup> T<sup>-b</sup>] Comparing powers of M, L and T, we get c = 1, 2a + b - 3c = 1 -b = -2 or b = 2Also, 2a + 1 - 3(1) = 12a = 2 or a = 1  $\Rightarrow$ This is 1, 2, 1 *.*..

8. In hydrogen atom, an electron jumps from bigger orbit to smaller orbit so that radius of smaller orbit is one-fourth of radius of bigger orbit. If speed of electron in bigger orbit was v then speed in smaller orbit is

(C) v

(D) 2v

,ounp

(A) V	(D) V
(A) $\frac{V}{4}$	(B) $\frac{V}{2}$
4	2

Ans. (D)

Sol. Radius of nth orbit  $r_n \propto n^2$ 

> $\frac{r_{n} \text{ big}}{r_{n} \text{ small}} = \frac{n_{\text{big}}^{2}}{n_{\text{small}}^{2}} = \frac{4}{1}$ (given)

$$\Rightarrow \qquad \frac{n_{\text{big}}}{n_{\text{small}}} = 2 \Rightarrow \frac{n_{\text{small}}}{n_{\text{big}}} = \frac{1}{2}$$

IT-JEE Velocity of electron in nth orbit ()

$$v_n \propto \frac{1}{n}$$

= 2 ==

 $V_{n \text{ small}} = 2 (v_{n \text{ big}}) = 2v$ 

9. A steel wire of length 4.7m and cross-section  $3.0 \times 10^{-5}$  m<sup>2</sup> stretches by the same amount as a copper wire of length 3.5m and cross-section  $4.0 \times 10^{-5}$  m<sup>2</sup> under a given load. What is the ratio of the Young's modulus of steel so that of copper?

(A) 1.5:2 (B) 1.8 : 2 (C) 1.5 : 1 (D) 1.8:1

Ans. (D)

Sol. As given for steel wire

 $A_1 = 3 \times 10^{-5} \text{ m}^2$ ,  $\ell_1 = 4.7 \text{m}$ ,  $\Delta \ell_1 = \Delta \ell$ ;  $F_1 = F$ 

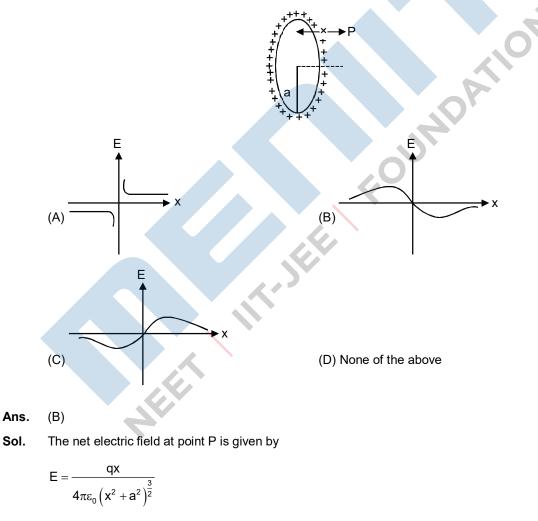
For copper wire,

 $A_2 = 4 \times 10^{-5} \text{ m}^2$ ,  $\ell_2 = 3.5 \text{m}$ ,  $\Delta \ell_2 = \Delta \ell$ ;  $F_2 = F$ 

Let Y<sub>1</sub> and Y<sub>2</sub> be the Young's modulus of steel wire and copper wire respectively.

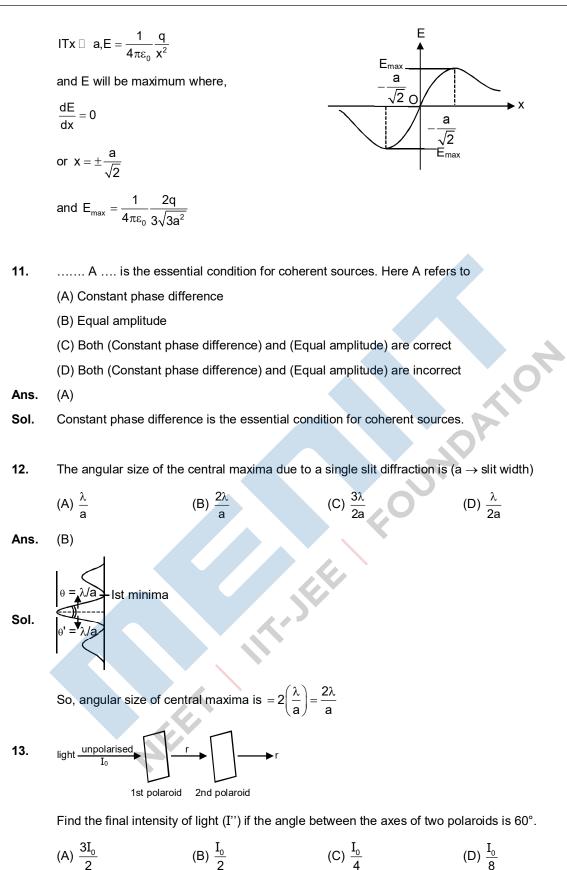
So, 
$$Y_1 = \frac{F_1}{A_1} \times \frac{\ell_1}{\Delta \ell_1} = \frac{F}{3 \times 10^{-5}} \times \frac{4.7}{\Delta \ell}$$
  
And  $Y_2 = \frac{F_2 \times \ell_2}{A_1 \times \Delta \ell_2} = \frac{F \times 3.5}{4 \times 10^{-5} \times \Delta \ell}$   
 $\frac{Y_1}{Y_2} = \frac{4.7 \times 4 \times 10^{-5}}{3.5 \times 3.0 \times 10^{-5}} = 1.8$   
So,  $Y_1 : Y_2 = 1.8 : 1$ 

10. A ring shaped conductor with radius a carries a net positive charge q uniformly distributed on it as shown in figure. A point P is situated at a distance x from its centre. Which of following graph shows the correct variation of electric field (E) with distance (x)?



:. At centre of ring x = 0  $\Rightarrow$  E<sub>0</sub>

Sol.



Ans. (D)

Sol. From first polaroid the unpolarised light will become polarized with half the intensity.

So, I' = 
$$\frac{I_0}{2}$$

From second polaroid

$$I'' = I'\cos^2\theta = \frac{I_0}{2}\cos^2(60) = \frac{I_0}{2}\frac{1}{4} = \frac{I_0}{8}$$

14. Resolving power of a telescope will be more, if the diameter (a) of the objective is

(A) Larger

(B) Smaller (C) Resolving power does not depend on a (D) None of the above

Ans. (C)

Sol. RP ∝ a

15. Let binding energy per nucleon of nucleus is denoted as E<sub>bn</sub> and radius of nucleus is denoted as r. If mass number of nuclei A, B are 64 and 125 respectively, then

(A) 
$$r_A < r_B$$
,  $E_{bnA} < E_{bnB}$   
(B)  $r_A > r_B$ ,  $E_{bnA} > E_{bnB}$   
(C)  $r_A = \frac{4}{5} r_B$ ,  $E_{bnA} < E_{bnB}$   
(D)  $r_A < r_B$ ,  $E_{bnA} > E_{bnB}$   
(D)  $r_A < r_B$ ,  $E_{bnA} > E_{bnB}$ 

(C) 
$$r_A = \frac{4}{5} r_B, E_{bnA} < E_{bnB}$$
 (D)  $r_A < r_B, E_{bnA} > E_{bnB}$ 

Ans. (D)

**Sol.** 
$$r = r_0 (A)^{\frac{3}{2}}$$

r increases with increasing A = mass number So, r<sub>A</sub> < R<sub>B</sub> as mass number of A is smaller E<sub>bn</sub> decreases with increasing A for A > 56. <sup>56</sup>Fe has highest  $E_{bn}$  value.

So,  $E_{bn}$  for A = 64 is larger as compared to  $E_{bn}$  for nucleus with A = 125

 $E_{bnA} > E_{bnB}$ 

- 16. The heat energy (A) Is a state variable (B) Does not depend on the state of the system (C) Is equal to internal energy of the system (D) None of the above Ans. (B) Sol. Heat energy is not a state variable, it just energy in transition. 17. A current 4.0 A exist in a wire of cross-sectional area 2.0 mm<sup>2</sup>. If each cubic metre of the wire contains  $12.0 \times 10^{28}$  free electrons then the drift speed is (A) 2 × 10<sup>-8</sup> m/s (B) 0.5 × 10<sup>-3</sup> m/s (C) 1.04 × 10<sup>-4</sup> m/s (D) None of these
- Ans. (C)

Sol. The current density in the wire is The drift speed is

$$v = \frac{j}{hc} = \frac{2 \times 10^{6}}{12 \times 10^{28} \times 1.6 \times 10^{-19}}$$
$$= \frac{10^{6}}{6 \times 1.6 \times 10^{9}} = 1.04 \times 10^{-4} \,\text{m/s}$$

18. In an experiment on the specific heat of a metal a 0.20 kg block of the metal at 150°C is dropped in a copper calorimeter (of water equivalent 0.025kg) containing 150 cc of water at 27°C. The final temperature is 40°C. Calculate the specific heat of the metal. If heat losses to the surroundings are not negligible, is our answer greater or smaller than the actual value of specific heat of the metal?

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(A) 0.02	(B) 0.02	(C) 0.01	(D) 0.1
(,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	(12) 0.01	(0) 0.01	(2) 0.1

Ans. (D)

Sol. Mass of metal m = 0.2 kg = 200g

Fall in temperature of metal

 $\Delta T = 150 - 40 = 40^{\circ}C$ 

If s is specific heat of metal, the heat lost by the metal

 $\Delta Q = ms \Delta T = 200 \times 110 \times s$ 

Volume of water = 150 cc

Mass of water m' = 150g

Water equivalent of calorimeter

w = 0.025kg = 25g

Rise in temperature of water in calorimeter t-JEE

Heat gained by water and calorimeter

 $\Delta Q' = 175 \times 13 = \Delta Q$ 

So, 200 × s × 100 = 175 × 13

$$\Rightarrow \qquad \mathbf{s} = \frac{175 \times 13}{200 \times 100} \approx 0.1$$

Electric field in a region is given by  $E = \left(\frac{M}{x^s}\right)\hat{i}$ , then the correct expression for the potential in the region 19. is (assume potential at infinity is zero).

(A)  $\frac{M}{2x^2}$  (B) Mx<sup>2</sup> (C)  $\frac{M}{3x^4}$ (D) None of these

(A) Ans.

Sol. 
$$v(x,y,z) = -\int_{-\infty}^{(x,y,z)} E \cdot dr$$
  
 $= -\int_{-\infty}^{(x,y,z)} \frac{Mdx}{x^3} = \frac{M}{2x^2}$   
20. A ball is projected upwards from the top of tower with a velocity 50 m/s making an angle 30° with the horizontal. The height of tower is 70m. After how many seconds from the instant of throwing will the ball reach the ground?  
(A) 2 s (B) 5 s (C) 7 s (D) 9 s  
Ans. (C)  
Sol. Taking vertical downward motion of projectile from point of projection to ground we have,  
 $u = -50 \sin 30^\circ = -25 m/s$   
 $a = +10 m/s^2$ ,  $s = 70m$ ,  $t = ?$   
 $s = ut + \frac{1}{2}at^2$   
So,  $70 = -25 \times t + \frac{1}{2} \times 10 \times t^2$   
or  $5t^2 - 25t - 70 = 0$   
or  $t^2 - 5t - 14 = 0$   
On solving  $t = 7s$   
21. Three capacitors  $X = 1\mu F$ ,  $Y = 2\mu F$  and  $Z = 3\mu F$  are connected as shown in figure, then the equivalent capacitance between points A and B is

(A) 6 μF

(B) 12 μF

(D) None of these

Ans. (A)

Sol. The equivalent circuit of the following figure is as follow.



22.The work done in blowing a soap bubble of surface tension 0.06 Nm<sup>-1</sup> from 2cm radius to 5cm radius is(A) 0.004168 J(B) 0.003168 J(C) 0.003158 J(D) 0.004568 J

(C) 3 µF

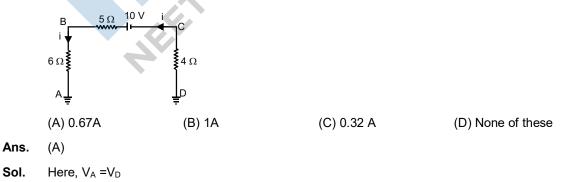
- Ans. (B)
- **Sol.** As given  $s = 0.06 \text{ Nm}^{-1}$

 $r_{1} = 2cm = 0.02m, r_{2} = 5cm = 0.05m$ Since, bubble has two surface Initial surface area of the bubble =  $2 \times 4\pi r_{2}^{2}$ =  $2 \times 4\pi \times (0.02)^{2} = 32\pi \times 10^{-4}m^{2}$ Final surface area of the bubble =  $2 \times 4\pi r_{2}^{2}$ =  $2 \times 4 \times \pi \times (0.05)^{2}$ =  $200 \times \pi \times 10^{-4} m^{2}$ So, work done = s × increase in surface =  $0.06 \times (200\pi \times 10^{-4} - 32\pi \times 10^{-4})$ =  $0.06 \times 168\pi \times 10^{-4}$ = 0.003168J

23. The sum of the magnitudes of two forces acting at a point is 16N. The resultant of these forces is perpendicular to the smaller force which has a magnitude of 8N. If the smaller force is magnitude x then the value of x is

	(A) 2N	(B) 4N	(C) 6N	(D) 7N
Ans.	(C)			.O <sup>v</sup>
Sol.	x + y = 16,			2
	Also, $y^2 = 8^2 + x^2$			
	or $y^2 = 64 + (16 - y)^2$	8N	y C	
	(∵ x = 16 − y)			
	or $y^2 = 64 + 256 + y^2 - 3$	32y		
	or 32y = 320		X	
	Y = 10 N		<b>)</b>	
	$\therefore$ x + 10 = $\Rightarrow$ x =6N			

24. What will be the value of current i in the circuit shown?



Since, points A and D are centred.

 $-6i - 5i + 10 - 4i = 0 \implies 15i = 10$  $\implies i = \frac{10}{15} = 0.67A$ 

= 1.8 × 1.5 × 1.2 cm<sup>3</sup>

25. The average depth of Indian Ocean is about 300m. Bulk modulus of water is 2.2 × 10<sup>4</sup> N/m<sup>2</sup>, g = 10 m/s<sup>2</sup>, then fractional compression  $\frac{\Delta V}{V}$  of water at the bottom of the Indian Ocean will be (A) 1.36% (B) 20.6% (C) 13.9% (D) 0.52% Ans. (A) Sol. The pressure exerted by a 3000m column of water on the bottom layer.  $P = h_{\rho}q = 3000 \times 1000 \times 10$ =  $3 \times 10^7$  kg, m<sup>-1</sup> s<sup>-2</sup> =  $3 \times 10^7$  N/m<sup>2</sup> Fractional compression  $\left(\frac{\Delta V}{V}\right)$  $=\frac{Stress}{B}=\frac{3\times10^7}{2.2\times10^9}$ JUNDATH = 1.36 × 10<sup>-2</sup>  $\frac{\Delta V}{V} \times 100 = 1.36\%$ Ans. (A) If <b>A</b> and <b>B</b> denote the sides of parallelogram and its area is  $\frac{1}{2}AB$  (A and B are 26. magnitude of <b>A</b> and <b>B</b> respectively), the angle between <b>A</b> and <b>B</b> is (A) 30° (B) 45° (C) 60° (D) 90° (A) Ans. Area of parallelogram | A × B | Sol.  $AB\sin\theta = \frac{1}{2}AB$  $\sin\theta = \frac{1}{2}, \theta = 30^{\circ}$ 27. If edge length of a cuboid are measured to be 1.2cm, 1.5cm and 1.8cm, then volume of the cuboid is (A) 3.240 cm<sup>3</sup> (B) 3.24 cm<sup>3</sup> (C) 3.2 cm<sup>3</sup> (D) 3.0 cm<sup>3</sup> Ans. (C) Sol. Volume of cuboid =  $\ell \times b \times h$ 

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= 2.70 × 1.2

= 3.240 cm<sup>3</sup>

Using concept of significant figures, product is reported in number of significant figures present in measurement which has least number of significant figures, here all measurement have 2 significant figures.

So, volume = 3.1 cm<sup>3</sup>

(keeping 2 significant figures only.)

28. A ball thrown upward from the top of a tower with speed v reaches the ground in t1 sec. If this ball is thrown downward from the top of the same tower with speed v it

reaches the ground in t<sub>2</sub> sec. In what time the ball shall reach the ground, if it is allowed to fall freely under gravity from the top of the tower?

.....(i)

.....(ii)

(A) 
$$\frac{t_1 + t_2}{2}$$
 (B)  $\frac{t_1 - t_2}{2}$  (C)  $\sqrt{t_1 t_2}$  (D)  $t_1 + t_2$   
(C)  
 $h = -vt_1 + \frac{1}{2}gt_1^2 \text{ or } \frac{h}{t_1} = v + \frac{1}{2}gt_1$  .....(i)  
 $h = -vt_2 + \frac{1}{2}gt_2^2 \text{ or } \frac{-h}{t_1} = -v + \frac{1}{2}gt_2$  .....(ii)  
 $\therefore \frac{h}{t_1} + \frac{h}{t_2} = \frac{1}{2}g(t_1 + t_2)$ 

Ans. (C)

 $h = -vt_1 + \frac{1}{2}gt_1^2 \text{ or } \frac{h}{t_1} = v + \frac{1}{2}gt_1$ Sol.

h = -vt<sub>2</sub> + 
$$\frac{1}{2}gt_2^2$$
 or  $\frac{-h}{t_1} = -v + \frac{1}{2}gt_2$   
∴  $\frac{h}{t_1} + \frac{h}{t_2} = \frac{1}{2}g(t_1 + t_2)$ 

or 
$$h = \frac{1}{2}gt_1t_2$$

For falls under gravity from the top of the tower  $h = \frac{1}{2}gt^2$ 

$$\begin{array}{ll} \therefore & \displaystyle \frac{1}{2}gt_1t_2 = \displaystyle \frac{1}{2}gt^2 \\ \\ \Rightarrow & \displaystyle t = \displaystyle \sqrt{t_1t_2} \end{array} \end{array}$$

One end of steel wire is fixed to ceiling of an elevator moving up with an acceleration 2 m/s<sup>2</sup> and a load 29. of 10kg hands from other end. Area of cross-section of the wire is 2 cm<sup>2</sup>. The longitudinal strain in the wire is  $(g = 10 \text{ m/s}^2 \text{ and } y = 2 \times 10^{11} \text{ Nm}^{-2})$ 

(A) 4 × 10<sup>11</sup> (B) 3 × 10 <sup>-6</sup> (C) 8 × 10<sup>−6</sup> (D) 2 × 10<sup>-6</sup>

**Sol.** As 
$$T = m(g + a_0) = 10 (10 + 2) = 120 N$$

Stress 
$$=\frac{T}{A} = \frac{120}{2 \times 10^{-4}} = 60 \times 10^{4} \text{ Nm}^{-2}$$

And 
$$Y = \frac{Stress}{strain}$$
, Strain =  $\frac{Stress}{Y}$   
=  $\frac{60 \times 10^4}{2 \times 10^{11}}$ 

= 30 × 10<sup>-7</sup> = 3 × 10<sup>-6</sup>

30. the electrostatic force of repulsion between two positively charged ions carrying equal charge is 3.7×10<sup>-9</sup>N, when they are separated by a distance of 5Å. How much electrons are missing from each ion?

**Sol.** Here,  $F = 3.7 \times 10^{-9} N$ 

Let,  $q_1 = q_2 = q$ r = 5Å = 5 × 10<sup>-10</sup>m

$$\therefore \mathsf{F} = \frac{1}{4\pi\varepsilon_0} \frac{\mathsf{q}_1\mathsf{q}_2}{\mathsf{r}^2}$$

$$\Rightarrow \qquad 3.7 \times 10^{-9} = 9 \times 10^9 \frac{q \times q}{(5 \times 10^{-10})^2}$$

$$q^{22} = \frac{3.7 \!\times\! 10^{-9} \!\times\! 25 \!\times\! 10^{-20}}{9 \!\times\! 10^{9}}$$

= 10.28 × 10<sup>-38</sup>

Now, q = ne

$$n = \frac{q}{e} = \frac{3.2 \times 10^{-19}}{1.6 \times 10^{-19}} = 2$$

**31.** A narrow beam of protons and deuterons, each having the same momentum, enters a region of uniform magnetic field directed perpendicular to their direction of momentum. The ratio of the radii of the circular paths described by them is

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(A) 1 : 2 (B) 1 : 1 (C) 2 : 1 (D) 1 : 3 (B)

**Sol.** Since the radius of circular path of charge particle of in magnetic field  $r = \frac{mv}{qB} = \frac{p}{qB}$ 

Now, the radius of circular path of charge particle of given momentum p and magnetic field B is given by

$$r \propto \frac{1}{q}$$

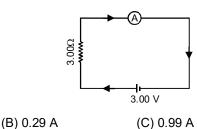
Ans.

But charge on both charge particles protons and deuterons, is same. Therefore,

 $\frac{r_{\rm p}}{r_{\rm D}} = \frac{q_{\rm D}}{q_{\rm p}} = \frac{1}{1}$ 

32. A solenoid of length 1.0m has a radius of 1cm and has a total of 1000 turns wound on it. It carries a current of 5A. If an electron were to move with a speed of  $10^4$  ms<sup>-1</sup> along the axis of this current carrying solenoid the force experienced by this electron is (A) 2N (B) 1.2N (C) zero (D) 2.5N (C) Ans. Sol. Here, L = 1m, N = 1000 The number of turn per unit length n = N/L = 1000 turn/m Magnetic field inside the solenoid  $B = \mu_0 nI = \mu_0 \times 1000 \times 5 = 2\pi \times 10^{-3} T$ The direction of magnetic field is along the solenoid. For electron q = -e,  $v = 10^4 \text{ ms}^{-1}$ Magnetic Lorentz force F =-evB sin 0° = 0 as the angle between B and v is 0° 33. Magnetic field (A) Can increase the speed of charge particle (B) Can accelerate a charge particle (C) Both (can increase the speed of charge particle) and (can accelerate a charge particle) are correct (D) Both (can increase the speed of charge particle) and (can accelerate a charge particle) are incorrect (B) Ans. Sol. Magnetic field can accelerate a charge particle by charging the direction of its velocity but it cannot change the speed of charged particle as magnetic force always acts perpendicular to the velocity of charged particle. 34. A square coil of side 10cm has 20 turn and carries a current of 12A. The coil is suspended vertically and the normal to the plane of the coil, makes an angle with  $\theta$  the direction of a uniform horizontal magnetic field of 0.80 T. If the torque, experienced by the coil, equals 0.96N-m, the value of  $\theta$  is (B)  $\frac{\pi}{2}$  radian (C)  $\frac{\pi}{3}$  radian (D)  $\frac{\pi}{6}$  radian (A) 0° (D) Ans. Area of coil A = side<sup>2</sup> =  $(0.1)^2 - 0.01m^2$ , Sol. Number of turns N = 20, current I = 12A, Normal to the coil make an angle  $\theta$  with the direction of B, magnetic field B = 0.80T Torque, experienced by the coil,  $\tau = 0.96 \text{ N} - \text{m}$ Since, total torque on the coil  $\tau = (NIA)B \sin \theta$ Substituting the values in above formula 0.96 N – m = 20 × 12 A ×  $0.01m^2 \times 0.80T \times \sin \theta$  $\sin \theta = \frac{0.96}{1.92} = \frac{1}{2}$  $\theta = \frac{\pi}{6}$  radian

**35.** In the circuit (figure) the current is to be measured. The ammeter shown is a galvanometer with a resistance  $R_G = 60.00\Omega$  converted to an ammeter by a shunt resistance  $rs = 0.02\Omega$ . The value of the current is



(D) 0.8 A

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Ans. (C)

(A) 0.79 A

**Sol.**  $R_g = 60.00\Omega$  shunt resistance  $r_s = 0.02\Omega$ 

Total resistance in the circuit is,

$$R_{G}$$
 + 3 = 63 $\Omega$ . Hence,  $I = \frac{3}{63} = 0.048A$ 

Resistance of the galvanometer converted to an ammeter is,

$$\frac{R_{G}r_{s}}{R_{G}+r_{s}}=\frac{60\Omega\!\times\!0.02\Omega}{\left(60+0.02\right)\Omega}=0.02\Omega$$

Total resistance in the circuit is,

Hence,  $\ell = \frac{3}{3.02} = 0.99 A$ 

**36.** The susceptibility of a magnetism at 300K is  $1.2 \times 10^{-5}$ . The temperature at which the susceptibility increases to  $1.8 \times 10^{-5}$  is

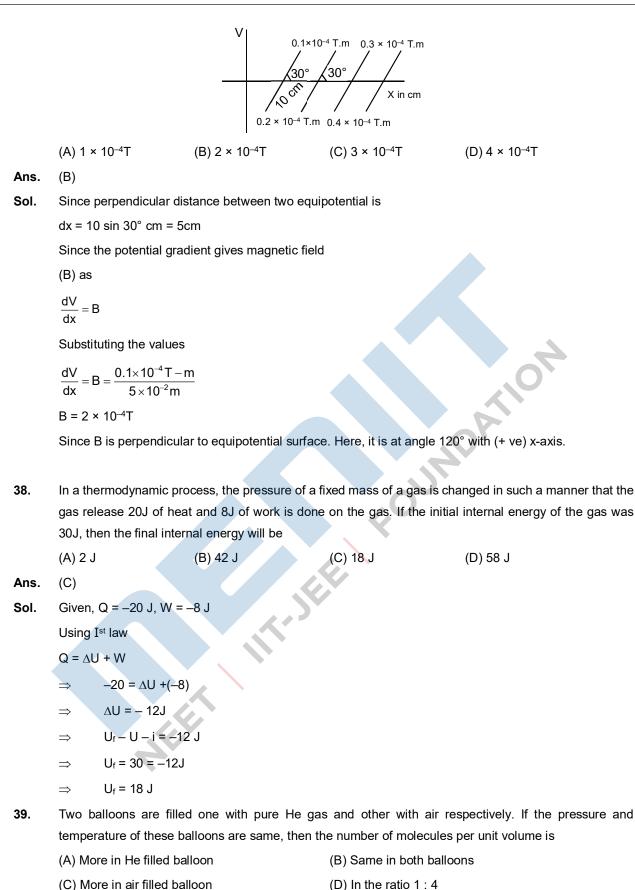
(A) 150 K (B) 200 K (C) 250 K (D) 20 K

Ans. (B)

Sol. x =

$$\Rightarrow \frac{1.2 \times 10^{-5}}{1.8 \times 10^{-5}} = \frac{T_2}{300}]$$
$$\Rightarrow T_2 = \frac{12}{18} \times 300 = 200K$$

**37.** Figure shows some of the equipotential surface of the magnetic scalar potential. The magnetic field <b>B</b> at a point in the region is



## Ans. (B)

- **Sol.** Assuming the balloons have the same volume, as pV = nRT. If p, V and T are the same, n the number of moles present will be the same, whether it is He or air. Hence, number of molecules per unit volume will be same in both the balloons.
- **40.** The equation of a simple harmonic motion is given by  $y = 3\sin\frac{\pi}{2}(50t x)$ , where x and y are in metres and t is in seconds, the ratio of maximum particle velocity to the wave velocity is

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(A) 
$$2\pi$$
 (B)  $\frac{3}{2}\pi$  (C)  $3\pi$  (D)  $\frac{2}{3}\pi$ 

Ans. (B)

Sol. The given wave equation is

$$y = 3\sin\frac{\pi}{2}(50t - x)$$
$$\Rightarrow y = 3\sin\left(25\pi t - \frac{\pi}{2}x\right) \dots (i)$$

Comparing with standard equation

$$\omega = 25\pi, k\frac{\pi}{2}$$

Wave velocity  $v = \frac{\omega}{K} = \frac{25\pi}{\frac{\pi}{2}} = 50 \text{m/s}$